

Quantum computing - climbing Mount Entanglement

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Classical and quantum mechanics

Macroscopic everyday phenomena are well described by classical physics.

Newton's laws
Maxwell Equations

At the microscopic level classical physics no longer works well.

Quantum mechanics takes over.

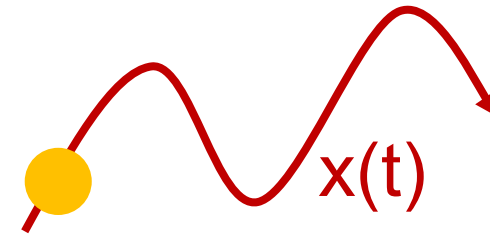
What is the difference between classical and quantum mechanics?

Quantum mechanics gives up on certainty and describes the world with amplitudes and probabilities.

Quantum uncertainty

Classical particles follow a path.

If we know $x(t_{\text{init}})$, and $p(t_{\text{init}}) = m v(t_{\text{init}})$



we can use Newton's laws of motion to calculate

$x(t)$ and $p(t) = m v(t)$ for all $t > t_{\text{init}}$.

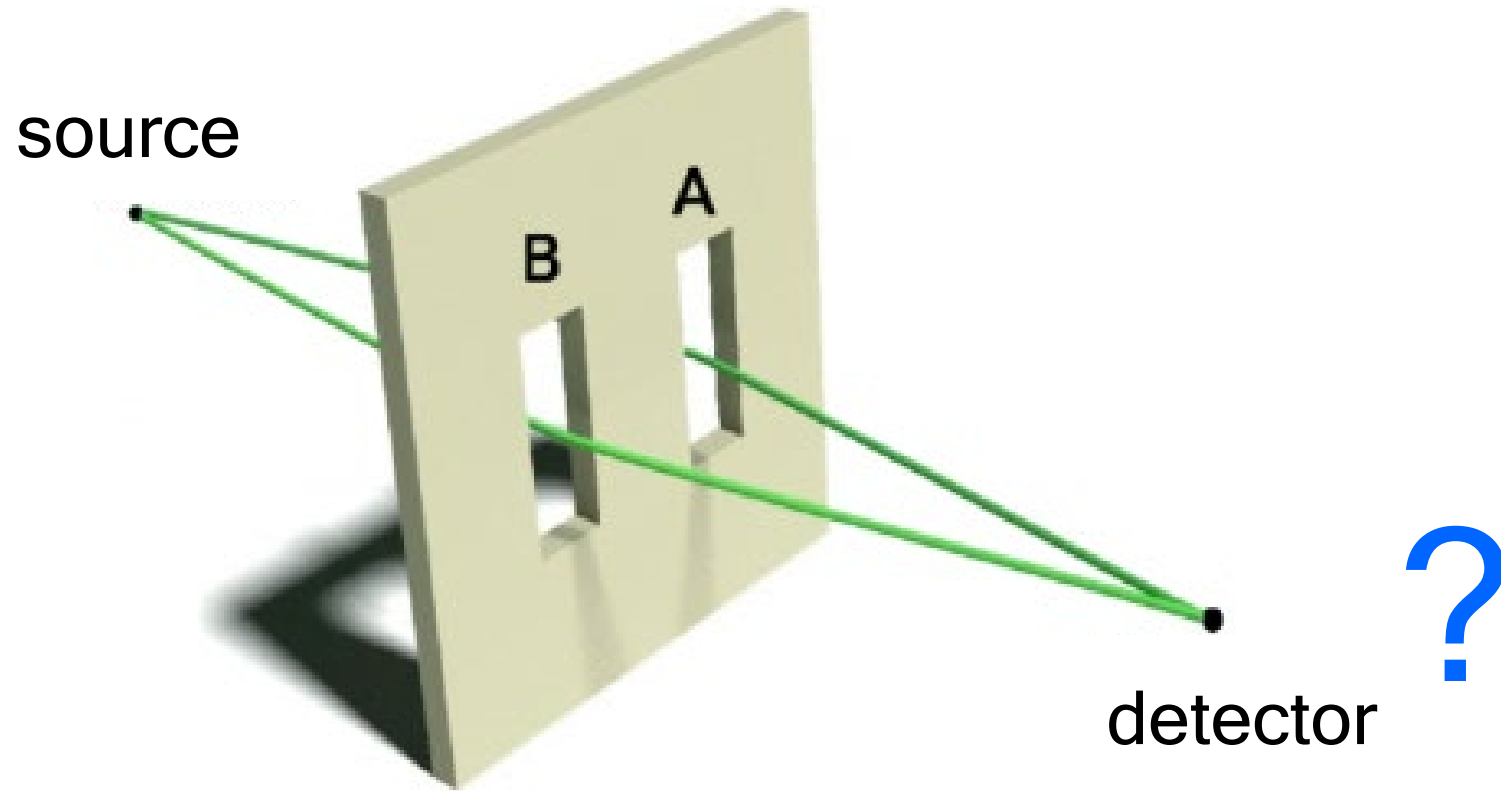
The motion is deterministic.

In quantum mechanics it is in principle NOT possible to know $x(t)$ AND $p(t)$ simultaneously.

Heisenberg uncertainty principle

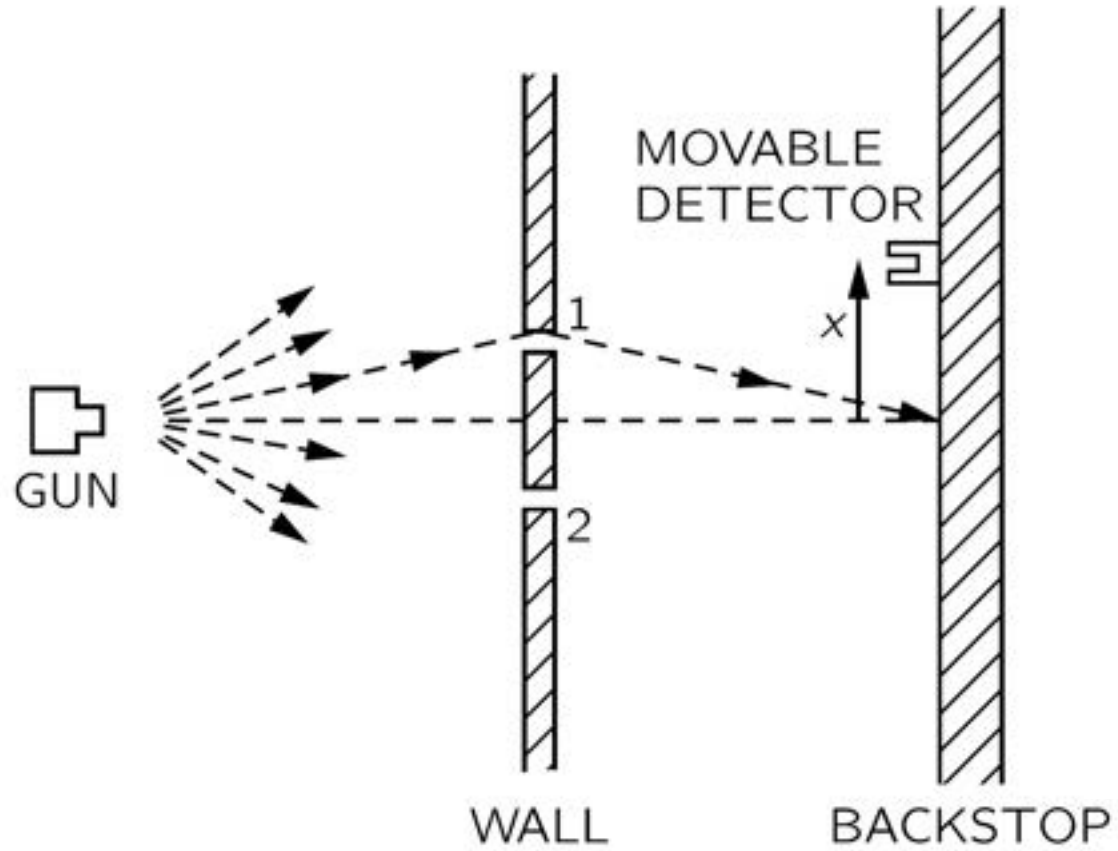
$$\Delta x \Delta p > \hbar / 2$$

Two slit experiment



Two slit experiment

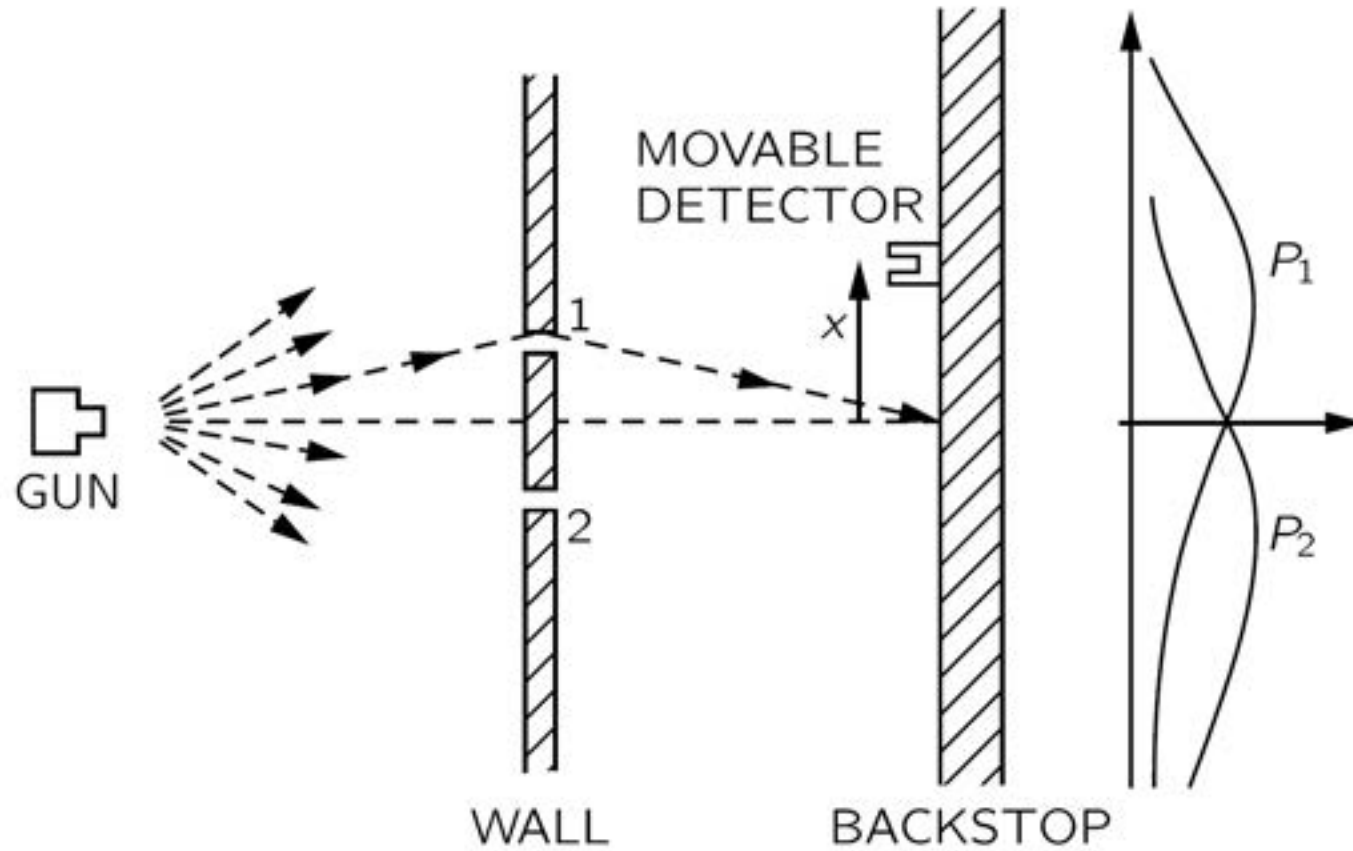
With classical particles:



?

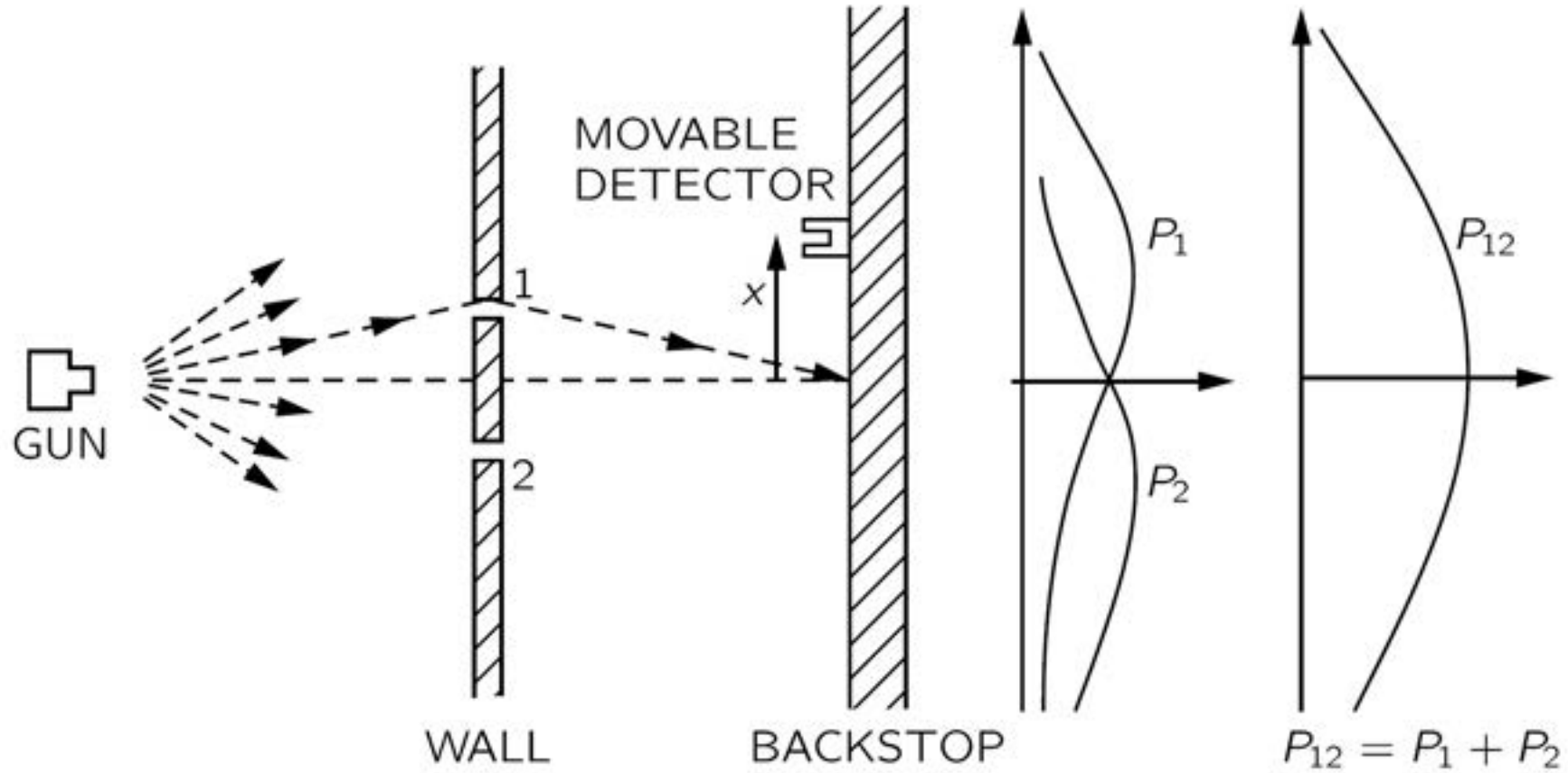
Two slit experiment

With classical particles:



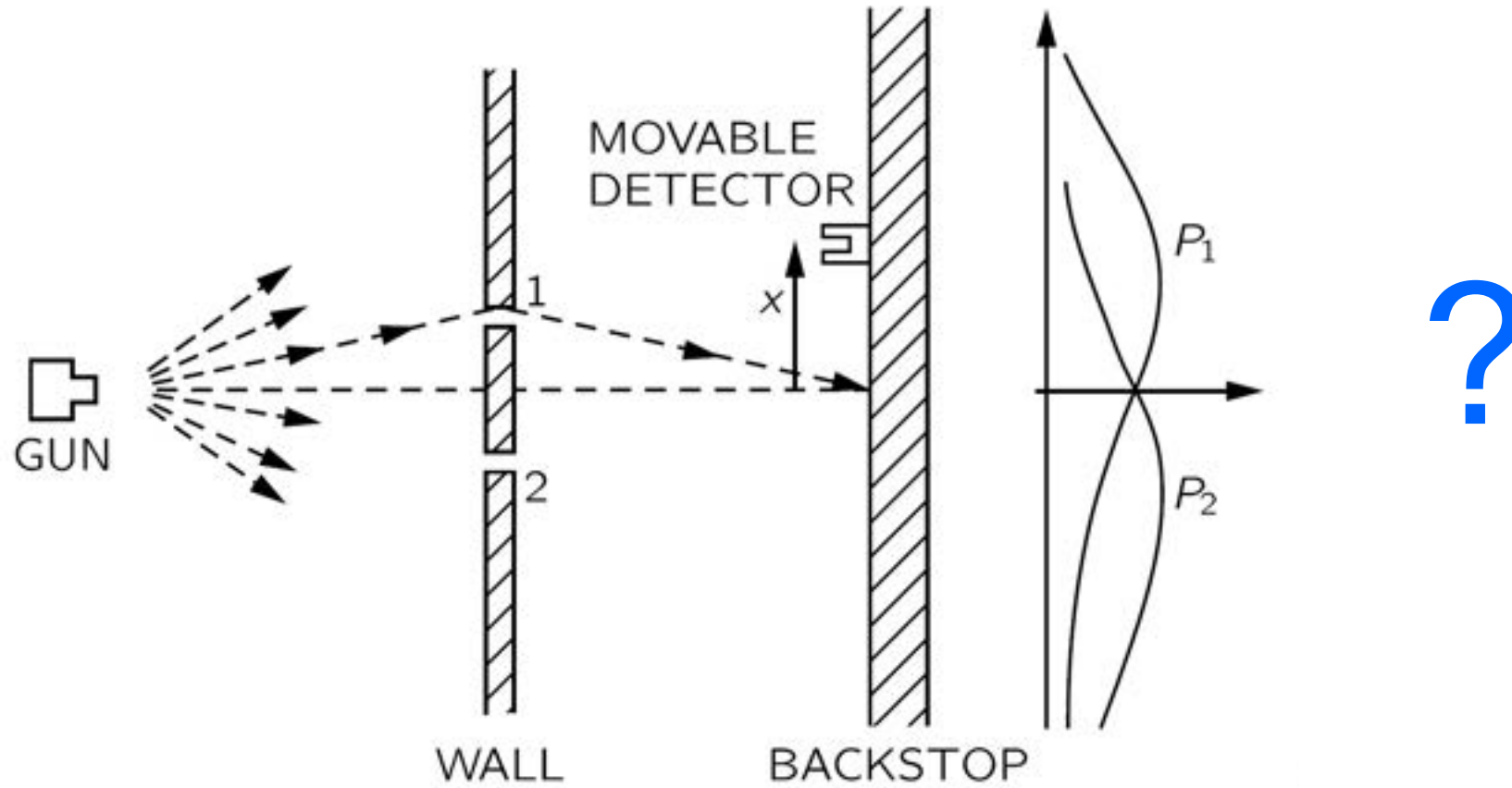
Two slit experiment

With classical particles:



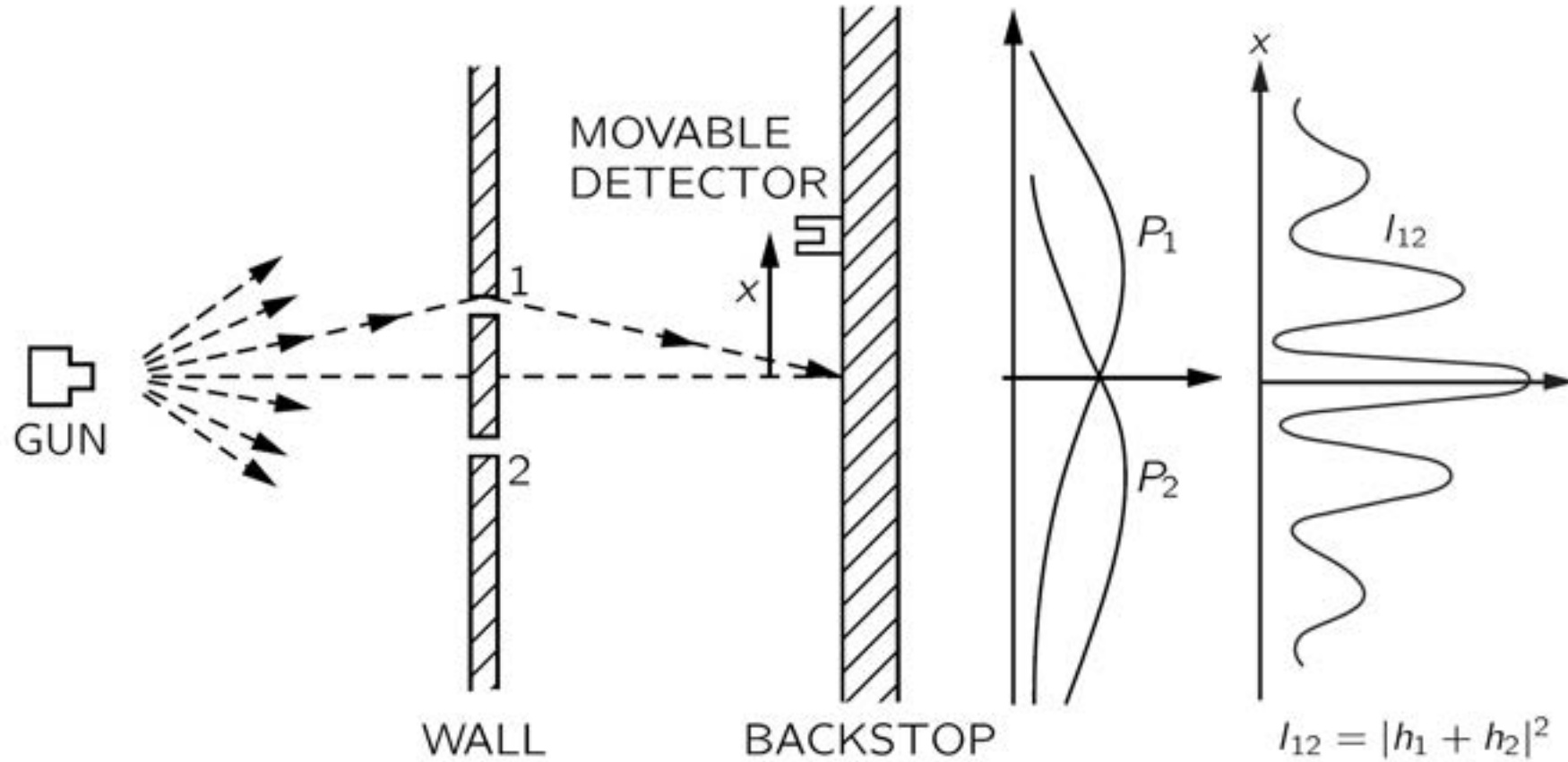
Two slit experiment

With quantum particles:



Two slit experiment

With quantum particles:



Two slit experiment

The experiment has been done.

Proceedings of the Cambridge Philosophical Society

Interference fringes with feeble light. By G. I. TAYLOR, B.A.,
Trinity College. (Communicated by Professor Sir J. J. Thomson,
F.R.S.)
[Read 25 January 1909.]



The phenomena of ionisation by light and by Röntgen rays have led to a theory according to which energy is distributed unevenly over the wave-front (J. J. Thomson, *Proc. Camb. Phil. Soc.* xiv. p. 417, 1907). There are regions of maximum energy widely separated by large undisturbed areas. When the intensity of light is reduced these regions become more widely separated, but the amount of energy in any one of them does not change; that is, they are indivisible units.

So far all the evidence brought forward in support of the theory has been of an indirect nature; for all ordinary optical phenomena are average effects, and are therefore incapable of differentiating between the usual electromagnetic theory and the modification of it that we are considering. Sir J. J. Thomson however suggested that if the intensity of light in a diffraction pattern were so greatly reduced that only a few of these indivisible units of energy should occur on a Huygens zone at once the ordinary phenomena of diffraction would be modified. Photographs were taken of the shadow of a needle, the source of light being a narrow slit placed in front of a gas flame. The intensity of the light was reduced by means of smoked glass screens.

Before making any exposures it was necessary to find out what proportion of the light was cut off by these screens. A plate was exposed to direct gas light for a certain time. The gas flame was then shaded by the various screens that were to be used, and other plates of the same kind were exposed till they came out as black as the first plate on being completely developed. The times of exposure necessary to produce this result were taken as inversely proportional to the intensities. Experiments made to test the truth of this assumption shewed it to be true if the light was not very feeble.

Five diffraction photographs were then taken, the first with direct light and the others with the various screens inserted between the gas flame and the slit. The time of exposure for the first photograph was obtained by trial, a certain standard of blackness being attained by the plate when fully developed. The

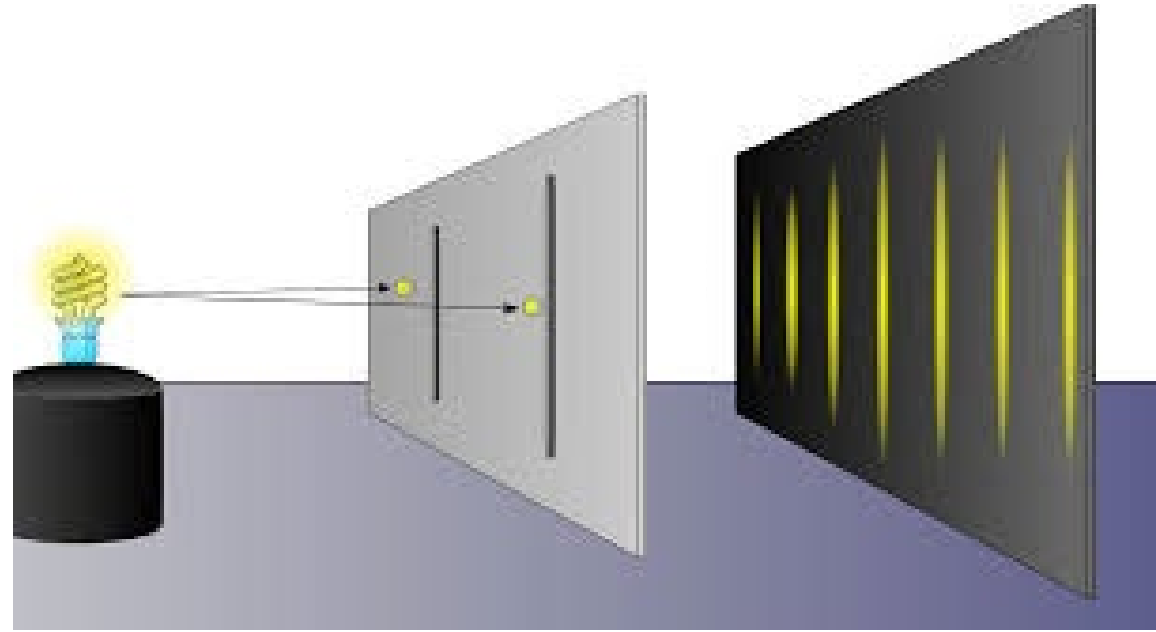
remaining times of exposure were taken from the first in the inverse ratio of the corresponding intensities. The longest time was 2000 hours or about 3 months. In no case was there any diminution in the sharpness of the pattern although the plates did not all reach the standard blackness of the first photograph.

In order to get some idea of the energy of the light falling on the plates in these experiments a plate of the same kind was exposed at a distance of two metres from a standard candle till complete development brought it up to the standard of blackness. Ten seconds sufficed for this. A simple calculation will shew that the amount of energy falling on the plate during the longest exposure was the same as that due to a standard candle burning at a distance slightly exceeding a mile. Taking the value given by Drude for the energy in the visible part of the spectrum of a standard candle, the amount of energy falling on 1 square centimetre of the plate is 5×10^{-6} ergs per sec. and the amount of energy per cubic centimetre of this radiation is 1.6×10^{-18} ergs.

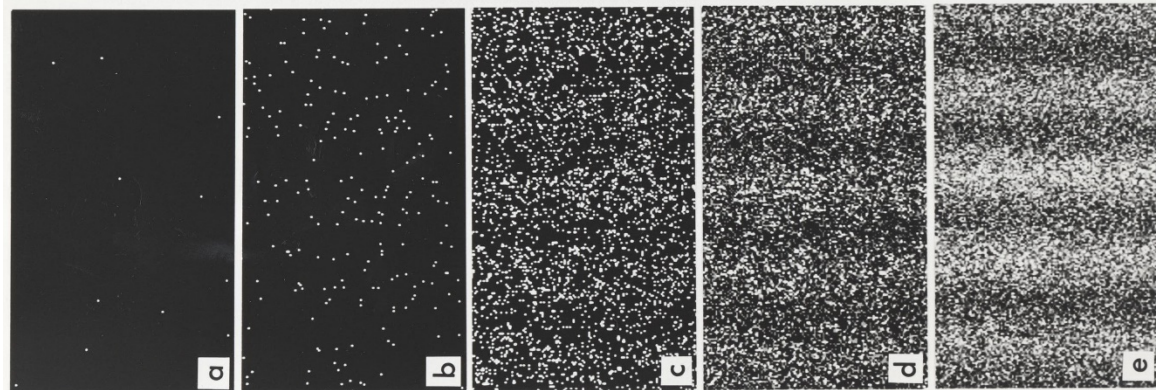
According to Sir J. J. Thomson this value sets an upper limit to the amount of energy contained in one of the indivisible units mentioned above.

Two slit interference with light

interference with
light waves



interference is
seen even when
only one photon at
a time passes the
slits



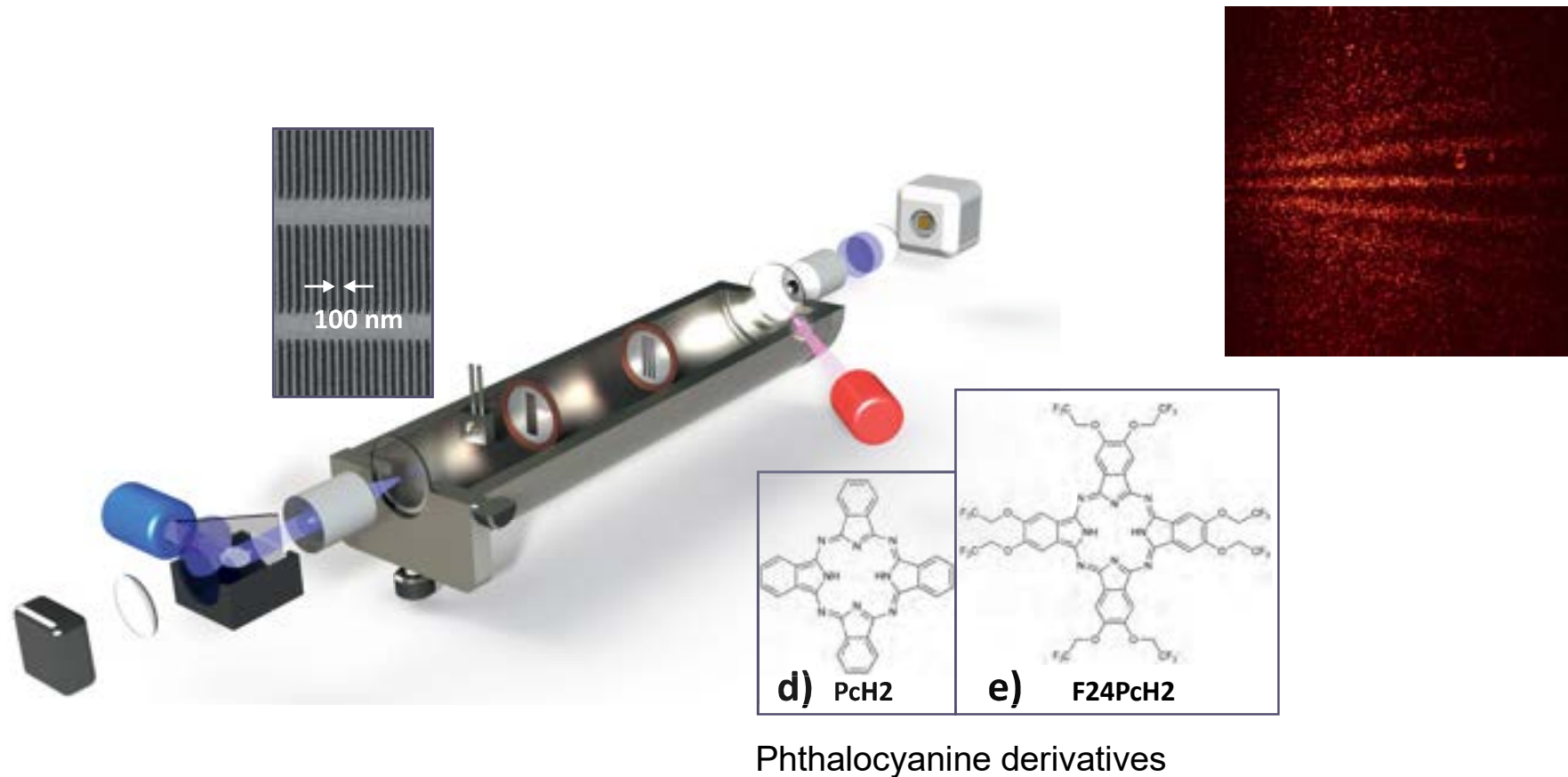
G.I. Taylor 1909

Quantum Spatial Superposition with Molecules

Interference fringes are observed.

Apparently each molecule propagates through both slits.

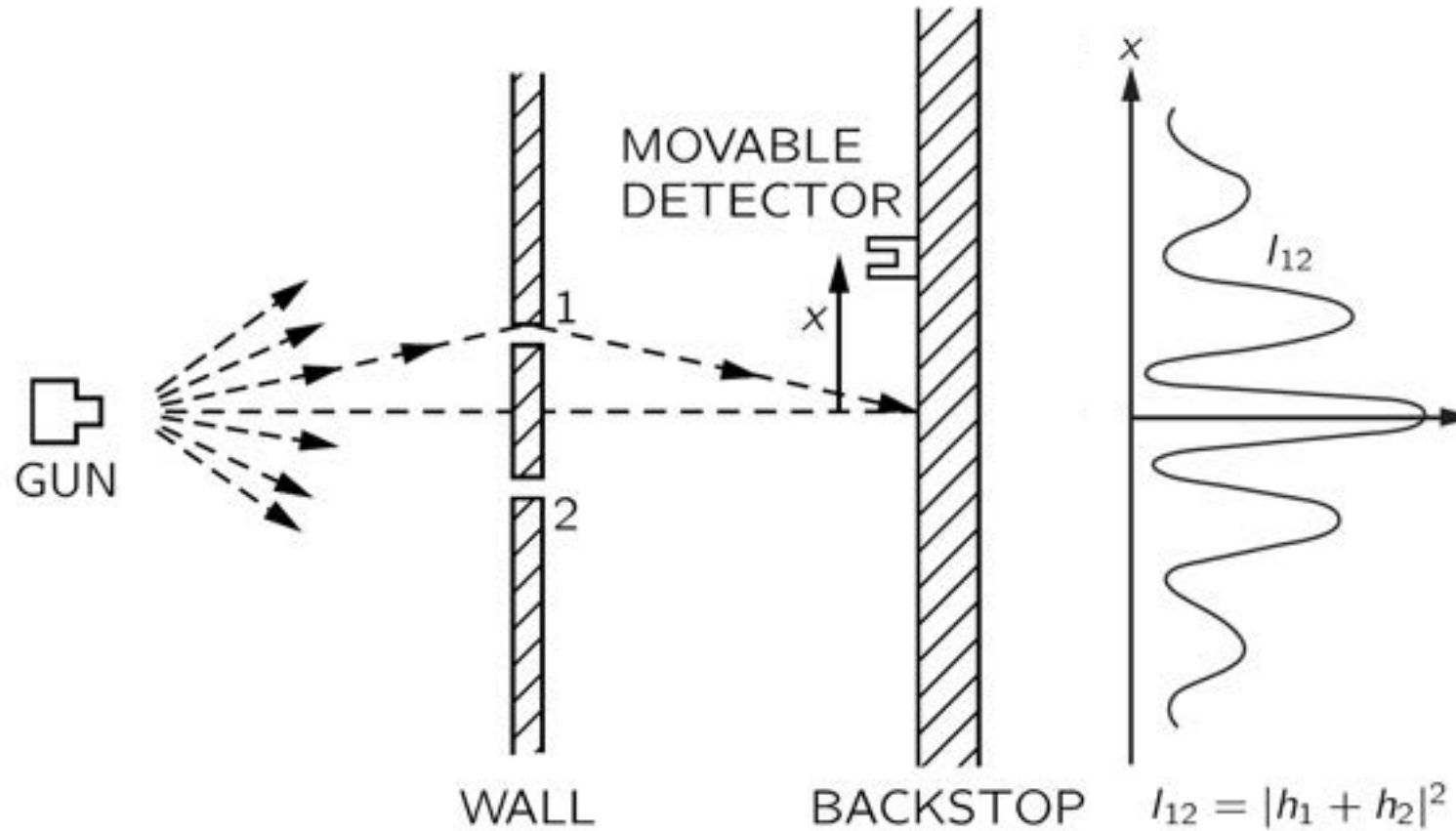
Quantum superposition of matter!



Two slit experiment

Experiment confirms interference.

How does the particle go through both slits?

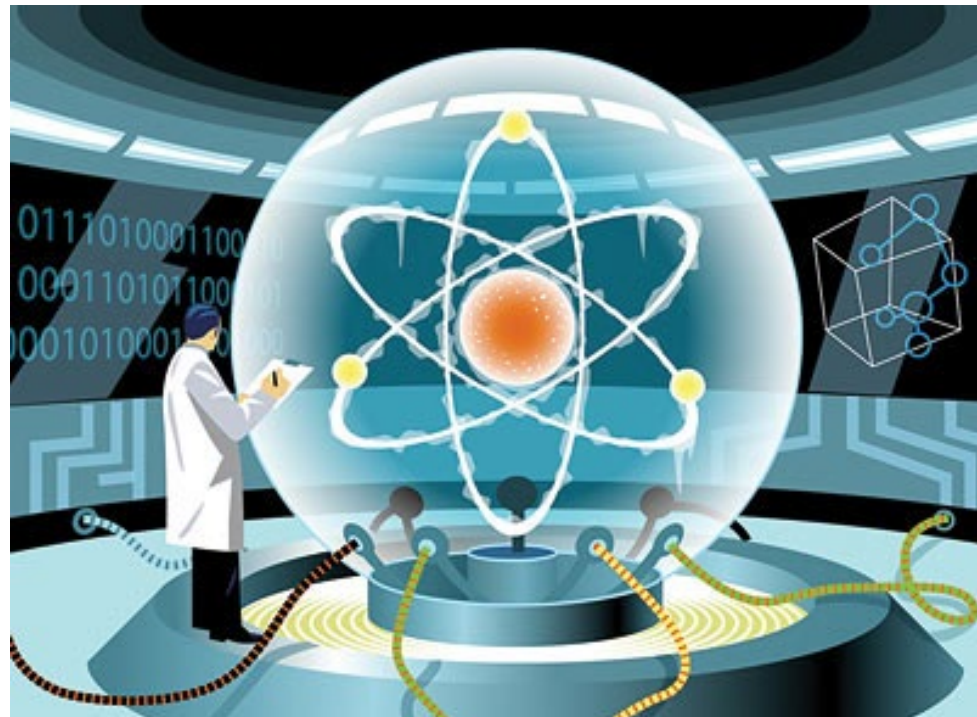


Quantum data

Not only can particles be in two places at once they can be used to represent two data values at once.

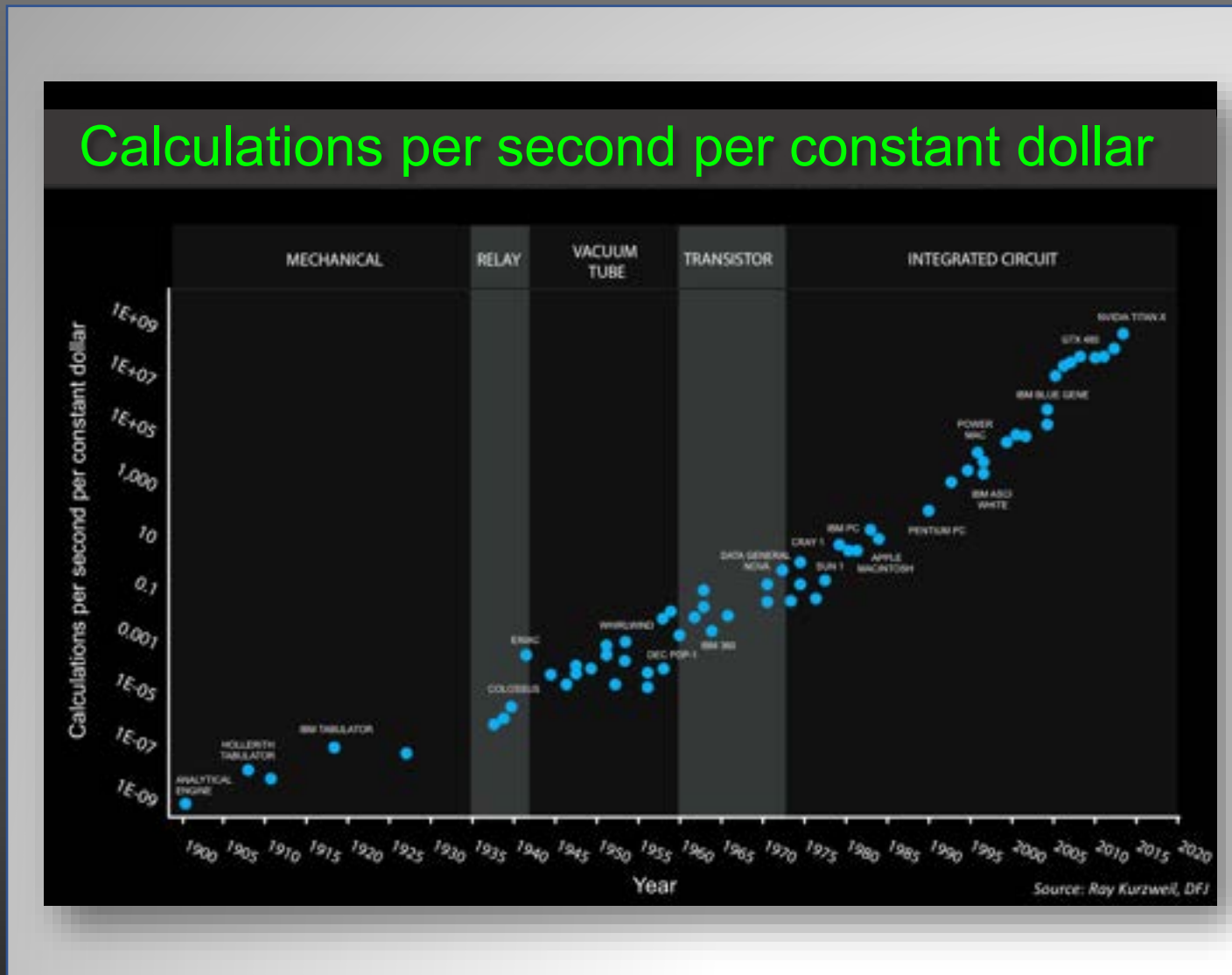
Qubits

Quantum computers



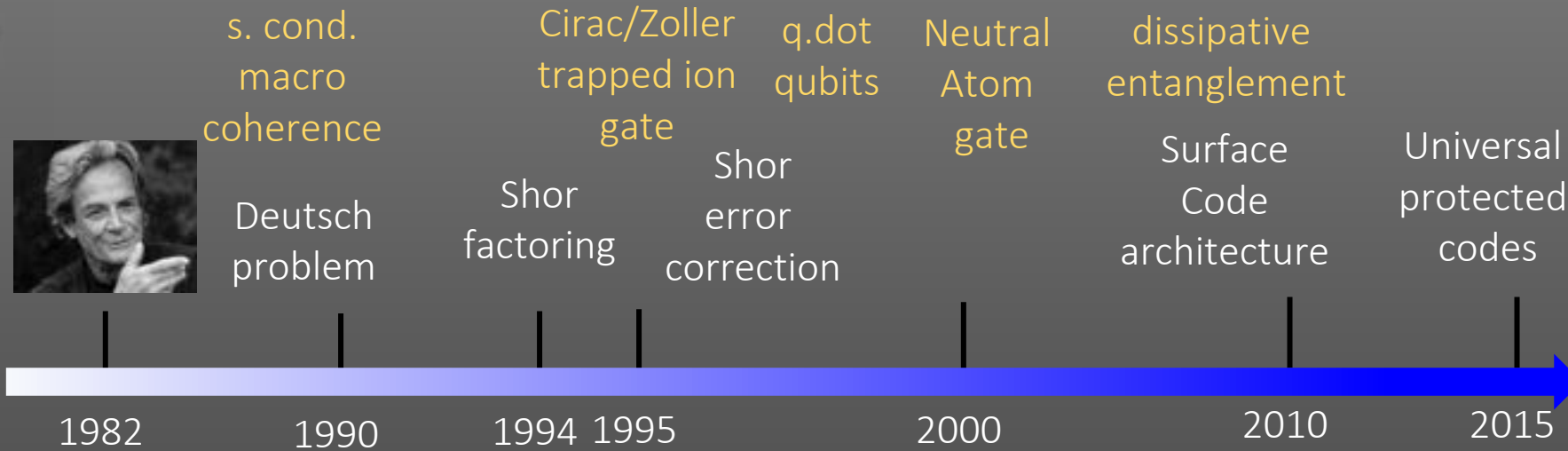
Moore's Law

- 5+ decades of exponential growth in computing power are drawing to a close.
- Quantum computers hold the promise of a new exponential advance over classical machines.
- Large government investments:
 - UK Quantum technology hubs £350M
 - European Union Quantum Flagship €1B
 - China National Lab for Quantum Information \$10B
 - US National Quantum Initiative \$1.25B
- Fortune 500 investments:
Google, Microsoft, IBM, Intel, Honeywell, Lockheed Martin, Raytheon,
- Startups:
DWave, Rigetti, Quantum Circuits, IonQ, Silicon Quantum Computing, ColdQuanta,...



Quantum computing timeline

Theory



Early 1980s: Richard Feynman and others propose quantum computers for tackling physics problems

1994: Peter Shor discovers a fast method to factor numbers on a quantum computer

Quantum: a new era in computing



Major investments on Quantum Computing research programmes from 2010 to 2016.

US National Strategy - NQI

A \$1.3B, five year investment in Quantum Information Science.



NATIONAL STRATEGIC OVERVIEW FOR QUANTUM INFORMATION SCIENCE

Product of the
SUBCOMMITTEE ON QUANTUM INFORMATION SCIENCE
under the
COMMITTEE ON SCIENCE
of the
NATIONAL SCIENCE & TECHNOLOGY COUNCIL

SEPTEMBER 2018

Quantum: a new era in computing



IBM Q™



What makes a
quantum
computer tick?

Quantum bits

Classical bits

0



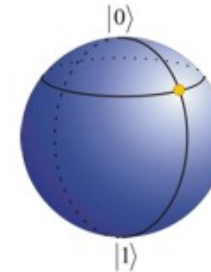
1



N classical bits can store a single data value out of 2^N possibilities.

Qubits

$$\text{data} = a|0\rangle + b|1\rangle$$



N qubits can store 2^N different values simultaneously. 2^{100} is more than the number of particles in the universe.

Quantum superposition !

Superposition and entanglement

Two qubits: $|\psi\rangle_1 = a_0|0\rangle + a_1|1\rangle, \quad |\psi\rangle_2 = b_0|0\rangle + b_1|1\rangle$

Product State: $|\psi\rangle = (a_0|0\rangle + a_1|1\rangle) \otimes (b_0|0\rangle + b_1|1\rangle)$
 $= a_0b_0|00\rangle + a_0b_1|01\rangle + a_1b_0|10\rangle + a_1b_1|11\rangle$


Classically we can only store one of four states at a time in a 2 bit memory: 00 or 01 or 10 or 11

$|\psi\rangle$ encodes four different states at one time.

With N qubits we can encode 2^N states at one time.

Superposition and entanglement

It is also possible to create states that are not product states:

$$|\psi\rangle = |00\rangle + |11\rangle \neq |\psi\rangle_1 |\psi\rangle_2$$




Verschränkung
"entanglement"

Such a state is entangled, and cannot be described in terms of classical bits – there is no local and realistic description of entangled states, Einstein, Podolsky, Rosen 1935 (EPR paradox).

Quantum computers provide a speedup over classical machines.

It is not clear exactly where the speedup comes from.

The power of quantum computers appears to be intimately related to the presence of entanglement. If there was no entanglement, we could use a classical description of the machine.

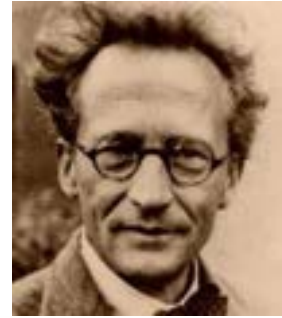
Superposition and entanglement

It is also possible to create states that are not product states:

$$|\psi\rangle = |00\rangle + |11\rangle \neq |\psi\rangle_1 |\psi\rangle_2$$



Maximally entangled 2-qubit state “Bell” state.



Verschränkung
“entanglement”

Physics Vol. 1, No. 3, pp. 195–200, 1964 Physics Publishing Co. Printed in the United States

ON THE EINSTEIN PODOLSKY ROSEN PARADOX*

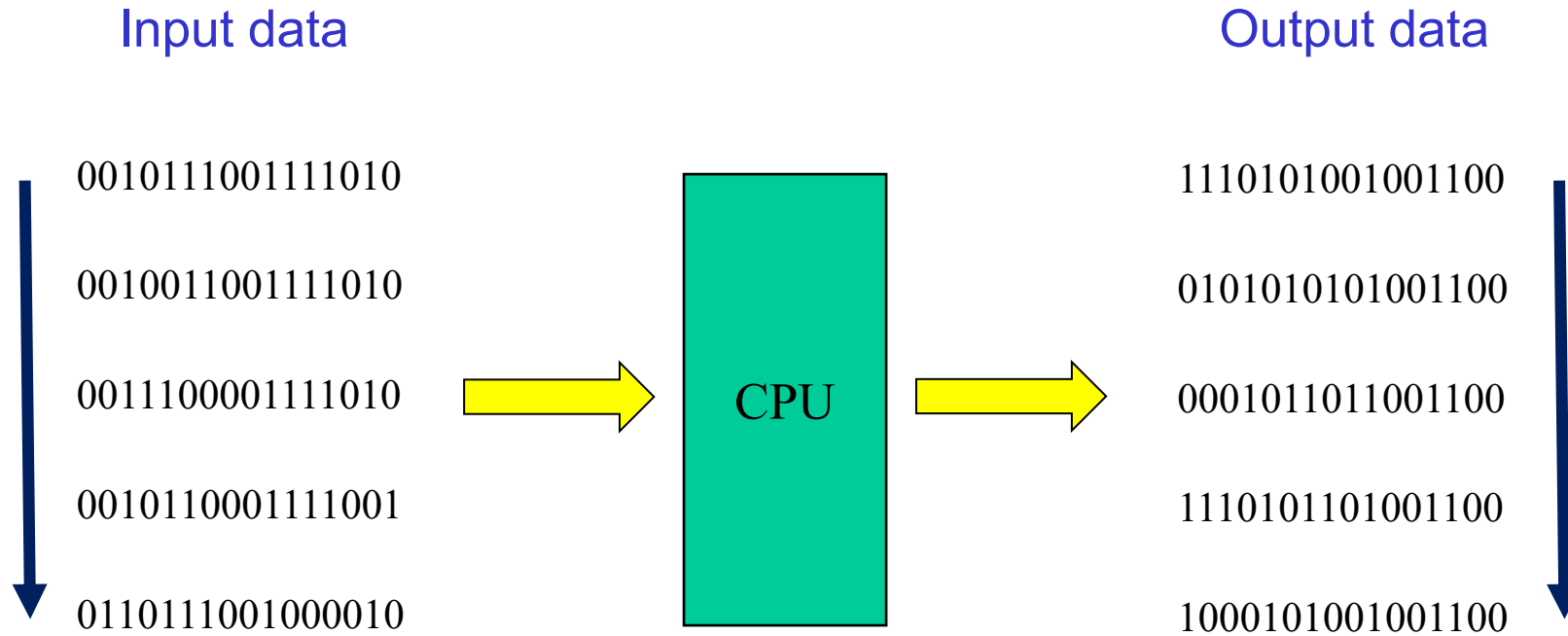
J. S. BELL[†]

Department of Physics, University of Wisconsin, Madison, Wisconsin

(Received 4 November 1964)



Classical data processing

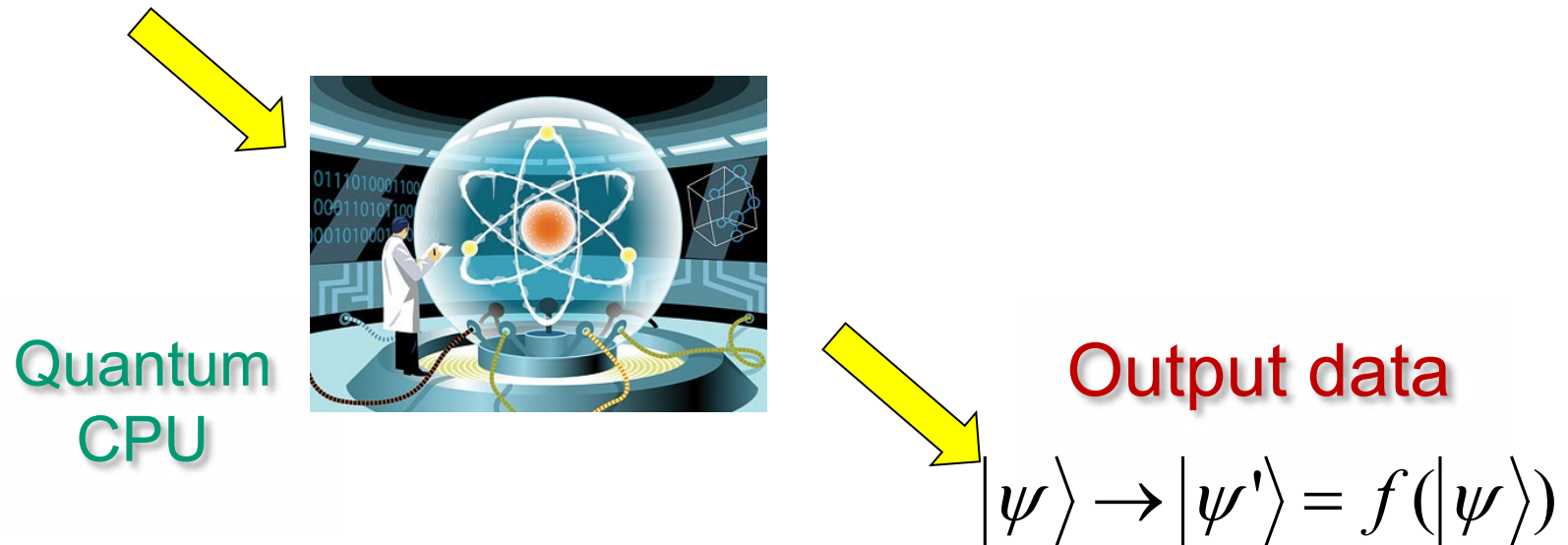


Sequential data processing

Quantum data processing

Input data

$$|\psi\rangle = a|00\dots00\rangle + b|00\dots01\rangle + c|00\dots10\rangle + d|00\dots11\rangle + \dots|11\dots11\rangle$$



$$|\psi'\rangle = a'|00\dots00\rangle + b'|00\dots01\rangle + c'|00\dots10\rangle + d'|00\dots11\rangle + \dots|11\dots11\rangle$$

The results for all possible input data are computed in parallel

But the result is only determined probabilistically

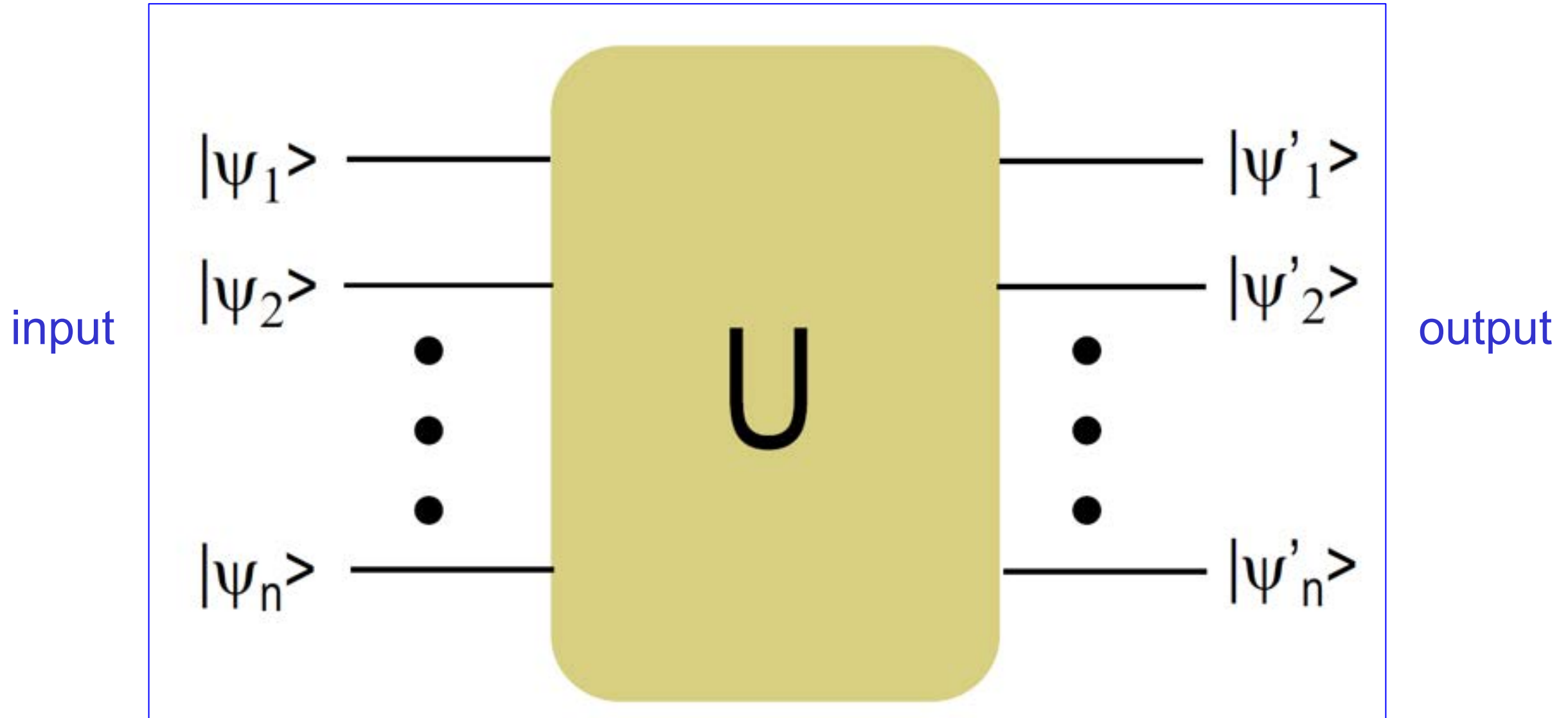
Running the computer



Output state (deterministic)							
	0	1	0	0	0	0	1
	1	1	0	0	1	1	1
measurement (probabilistic)	0	0	0	0	1	1	0
	0	0	1	0	1	0	1
	0	1	0	0	1	0	0

Quantum algorithms extract useful information from uncertain data.

Circuit model of Quantum Computing



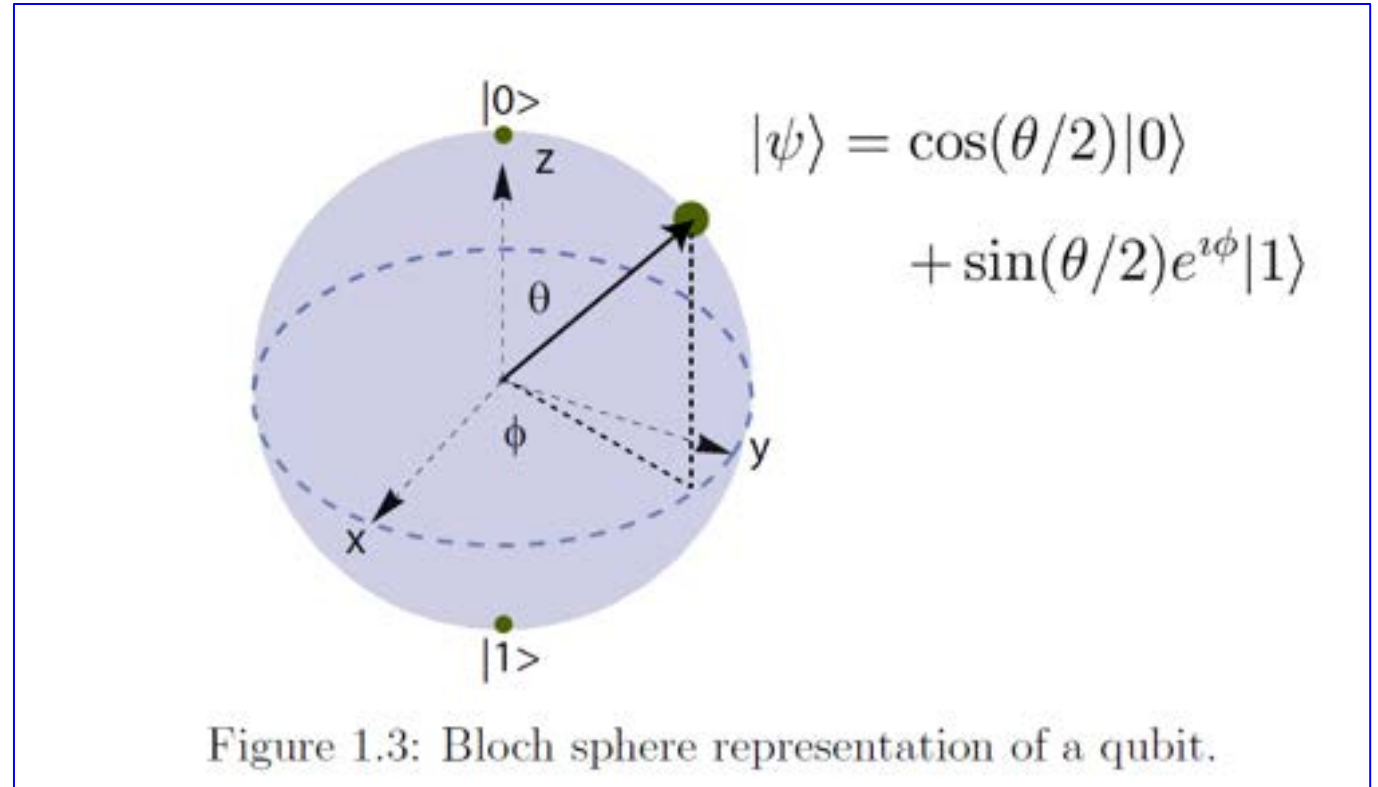
Arbitrary U can be decomposed into one- and two- qubit gates.

One-qubit gates

Qubit state can be parameterized by two angles on the Bloch sphere.

One-qubit gates rotate on the sphere.

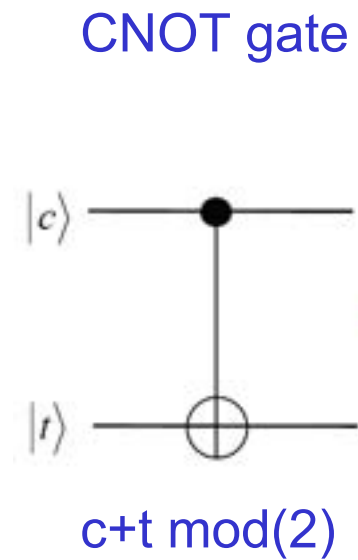
X gates rotate about x
Y gates rotate about y
Z gates rotate about z



Two-qubit gates

Two-qubit gates are required to create entanglement.

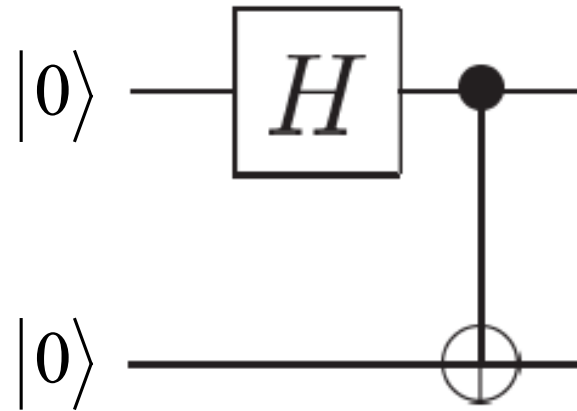
input	→	output
ct		ct
00		00
01		01
10		11
11		10



$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$

Entanglement on demand

We can create entanglement with a simple quantum circuit.



$$|00\rangle \xrightarrow{\text{H}} (|0\rangle + i|1\rangle)|0\rangle = |00\rangle + i|10\rangle \xrightarrow{\text{CNOT}} \boxed{|00\rangle + i|11\rangle}$$

HCNOTentanglement

Quantum Factoring algorithm

Peter Shor (1994 Bell labs)

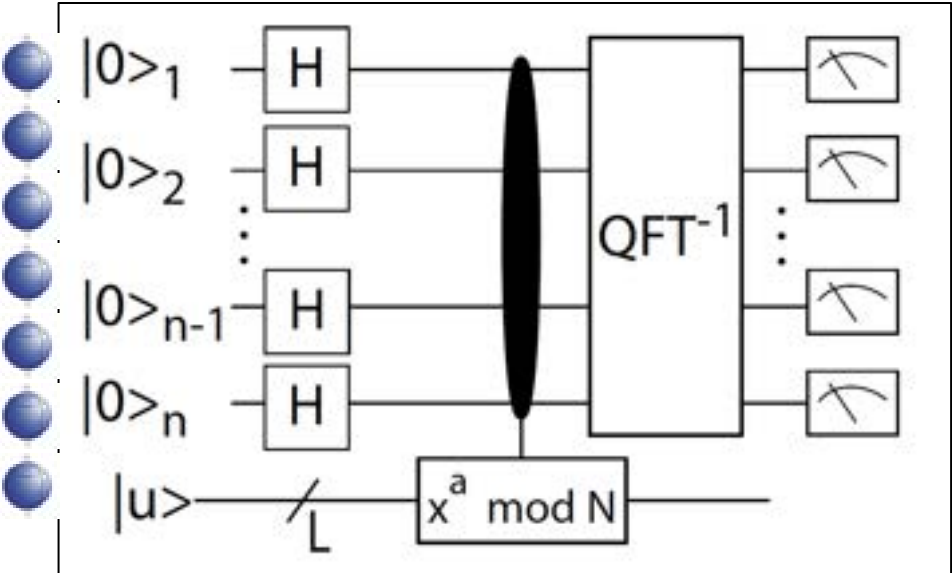


Best known classical algorithm:

$$time \sim e^{(\log N \log^2 N)^{1/3}}$$

Shor's quantum algorithm:

$$time \sim (\log N)^3$$



RSA Public key cryptography

- Rivest, Shamir, Adleman (RSA) invented a public key cryptosystem in 1977.
- Independently invented by C. Cocks in England in 1973 but kept secret.
- There is a public key known to everyone and a private key.
- Messages are encrypted with the public key and broadcast.
- Only recipients who know the private key can decrypt the message.
- This is widely used to protect personal data on the internet, e.g. online shopping.
- The security of RSA relies on the difficulty of factoring large numbers.



Factoring RSA Numbers

number	decimal digits	prize	factored (references)
RSA-100	100		Apr. 1991
RSA-110	110		Apr. 1992
RSA-120	120		Jun. 1993
RSA-129	129	\$100	Apr. 1994 (Leutwyler 1994, Cipra 1995)
RSA-130	130		Apr. 10, 1996
RSA-140	140		Feb. 2, 1999 (te Riele 1999a)
RSA-150	150		Apr. 6, 2004 (Aoki 2004)
RSA-155	155		Aug. 22, 1999 (te Riele 1999b, Peterson 1999)
RSA-160	160		Apr. 1, 2003 (Bahr et al. 2003)
RSA-200	200		May 9, 2005 (see Weisstein 2005a)
RSA-576	174	\$10000	Dec. 3, 2003 (Franke 2003; see Weisstein 2003)
RSA-640	193	\$20000	Nov. 4, 2005 (see Weisstein 2005b)
RSA-704	212	withdrawn	Jul. 1, 2012 (Bai et al. 2012, Bai 2012)
RSA-768	232	withdrawn	Dec. 12, 2009 (Kleinjung 2010, Kleinjung et al. 2010)
RSA-896	270	withdrawn	
RSA-1024	309	withdrawn	
RSA-1536	463	withdrawn	
RSA-2048	617	withdrawn	

Largest number known to have been factored:

RSA-768

=1230186684530117755130494958384962720772853569595334792197322452151726400507263657518
74520219978646938995647494277406384592519255732630345373154826850791702612214291346167
0429214311602221240479274737794080665351419597459856902143413

=

3347807169895689878604416984821269081770479498371376856891243388982883793878
002287614711652531743087737814467999489

x

367460436667995904282 4463379962795263227915816434308764267603228381573
9666511279233373417143396810270092798736308917

Classical number field
sieve algorithm

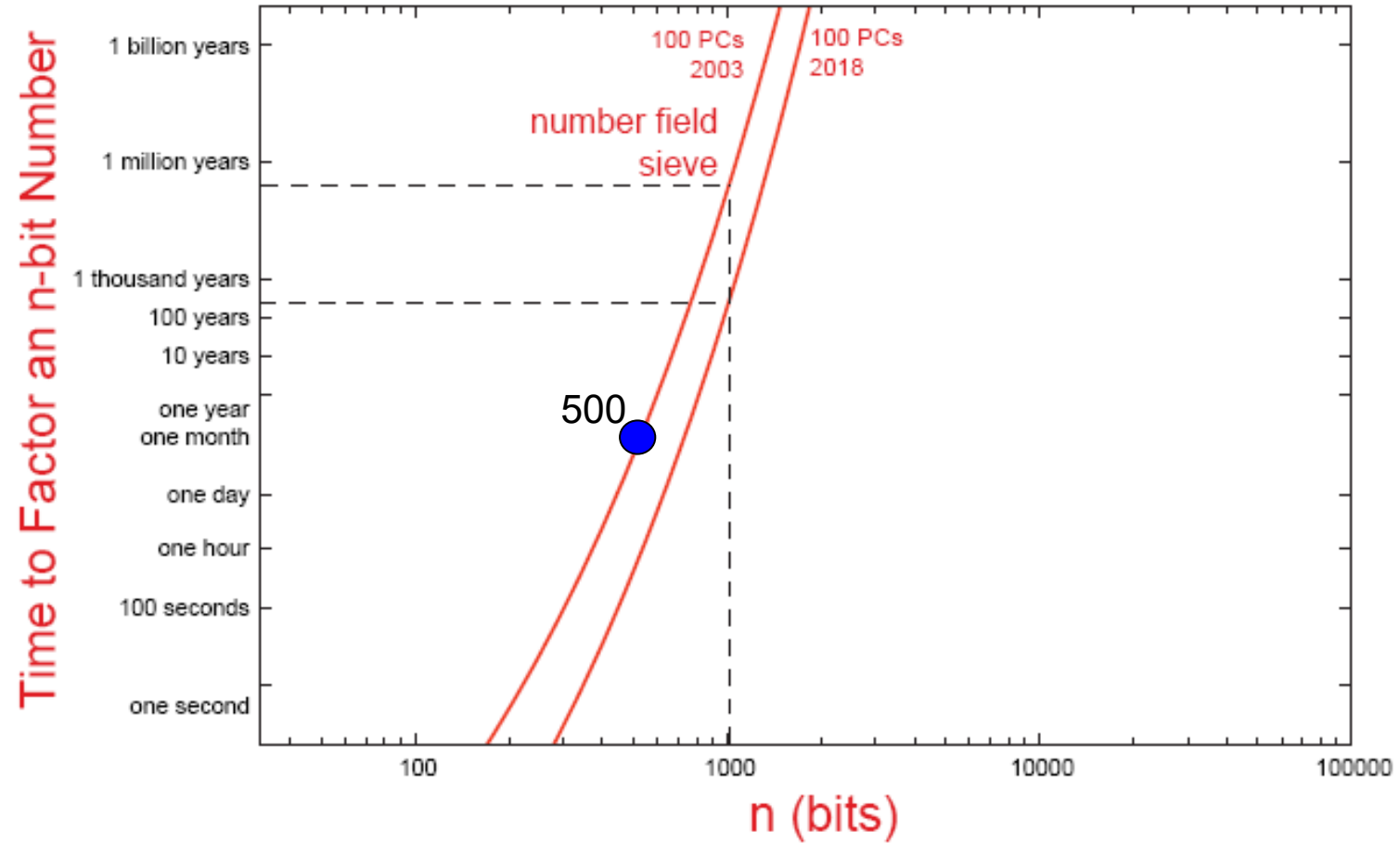
$$time \sim e^{1.9(\ln n)^{1/3} (\ln \ln n)^{2/3}}$$

RSA 768 took 1500
AMD64 years to
factor.

RSA 1536 would take
200 billion AMD64
years

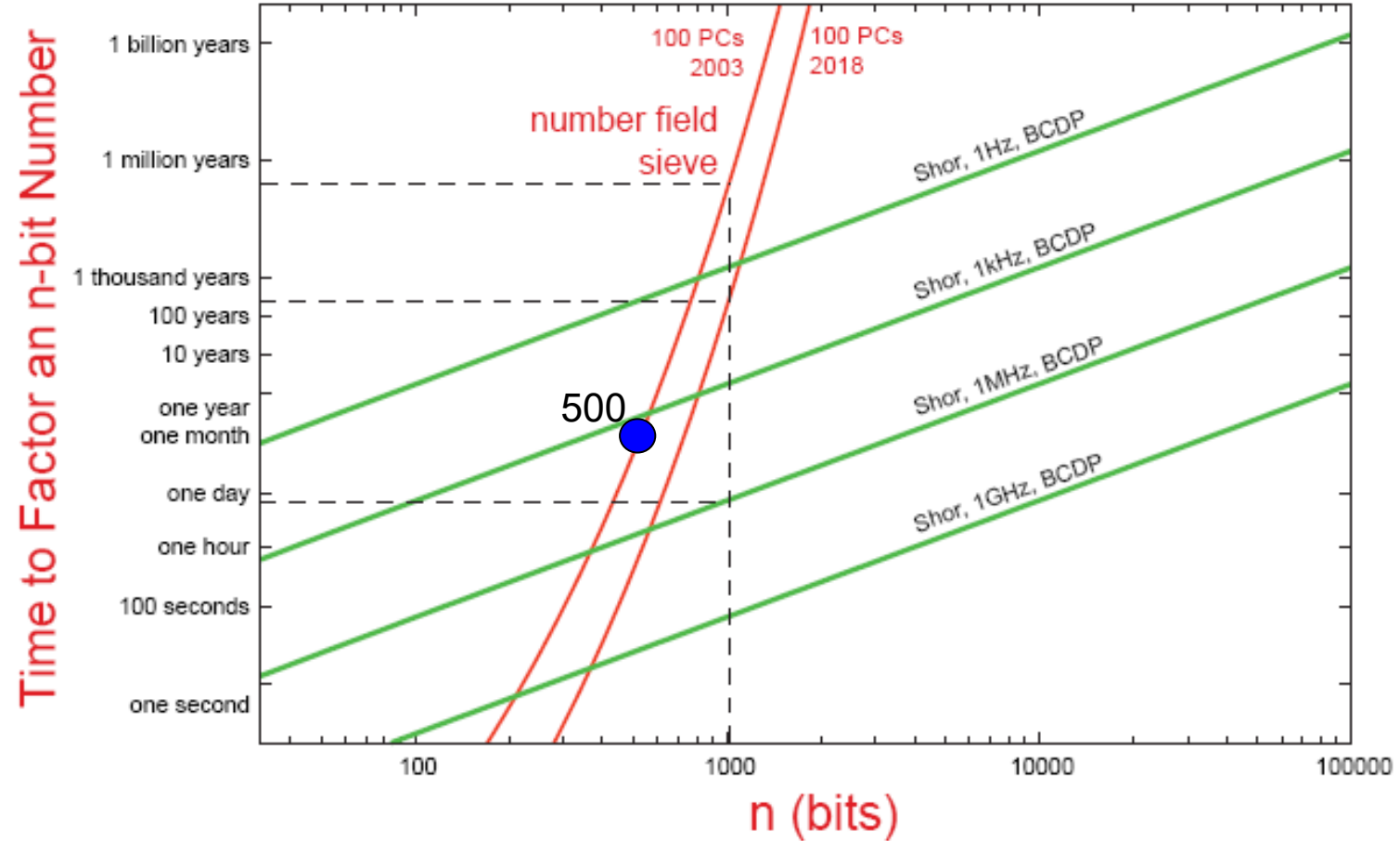
Factoring algorithms

vanMeter, et al. arXiv:quant-ph/0507023



Factoring algorithms

vanMeter, et al. arXiv:quant-ph/0507023



A simpler example: Deutsch-Jozsa

Consider the following problem. The function f takes a one bit input with value 0 or 1 and maps it to a one bit output, 0 or 1. There are four possibilities given in Table 3.1. The problem is to determine $f(0) \oplus f(1)$ which tells us whether the function is constant or balanced.

$f(0)$	$f(1)$	$f(0) \oplus f(1)$	type of function
0	0	0	constant
0	1	1	balanced
1	0	1	balanced
1	1	0	constant

Table 3.1: Truth table for a function f .
We refer to $f(0) = f(1)$ as a constant function and $f(0) \neq f(1)$ as balanced.

Classically this requires two evaluations of the function f . Using a quantum circuit we need only a single evaluation.

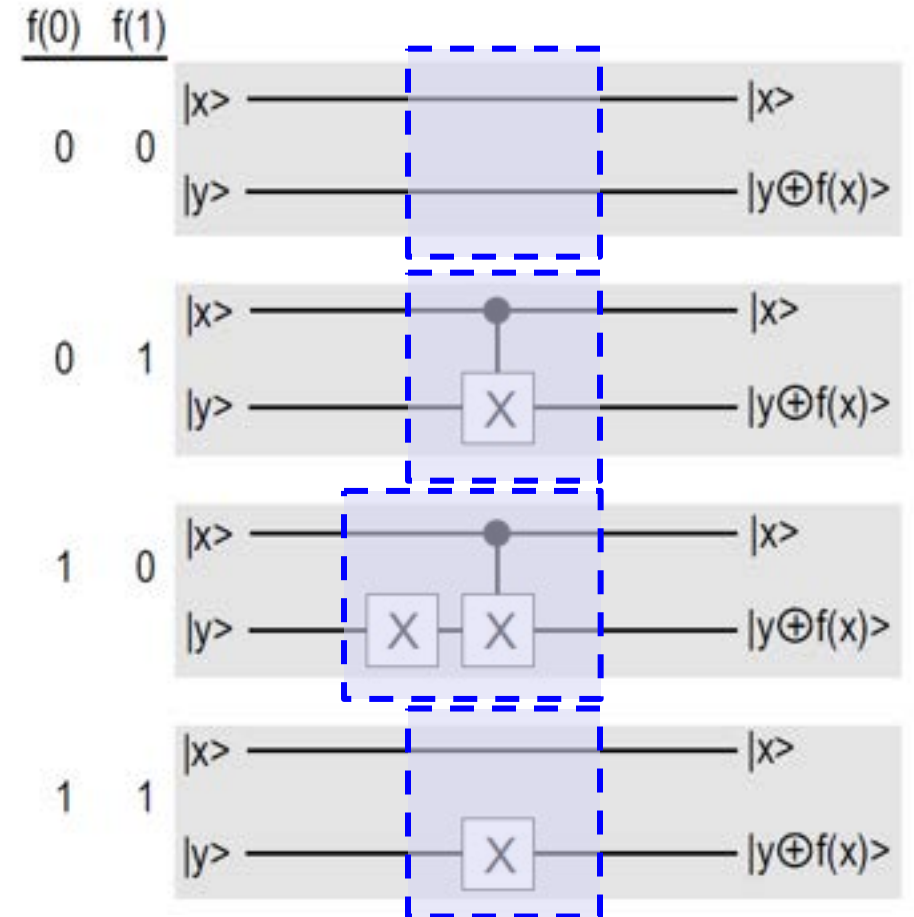
A simpler example: Deutsch-Jozsa

Classically this requires two evaluations of the function f . Using a quantum circuit we need only a single evaluation. The function evaluation can be expressed as a unitary operator

$$|x\rangle|y\rangle \xrightarrow{U_f} |x\rangle|y \oplus f(x)\rangle$$

Different $f(x)$ correspond to different quantum circuits.

Has been demonstrated in the lab.



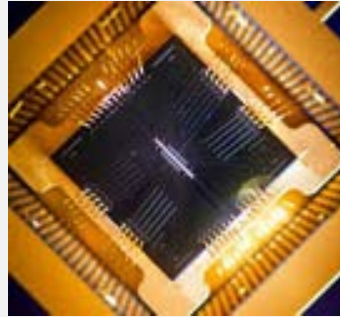
mount entanglement

How long is the road ?

Quantum Computing Platforms

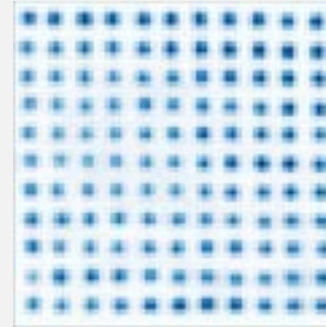
Atomic qubits (identical)
Room T apparatus (or 4K)
Optical interface/qu. networking
Laser cooling and control

trapped ions



~20Q demonstrated

neutral atoms



100Q arrays

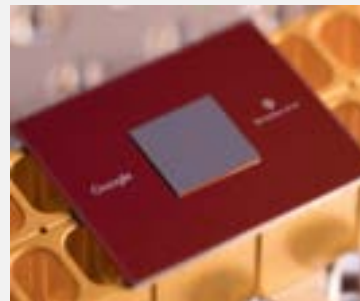
optical



Scalability challenging

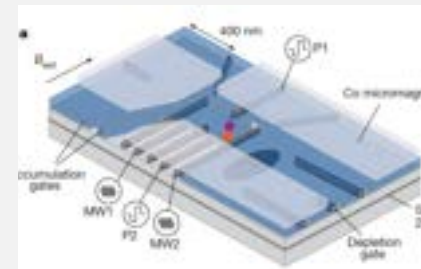
Engineered qubits (not identical)
Requires cryogenic cooling
No optical interface
Microwave electronics

superconductors

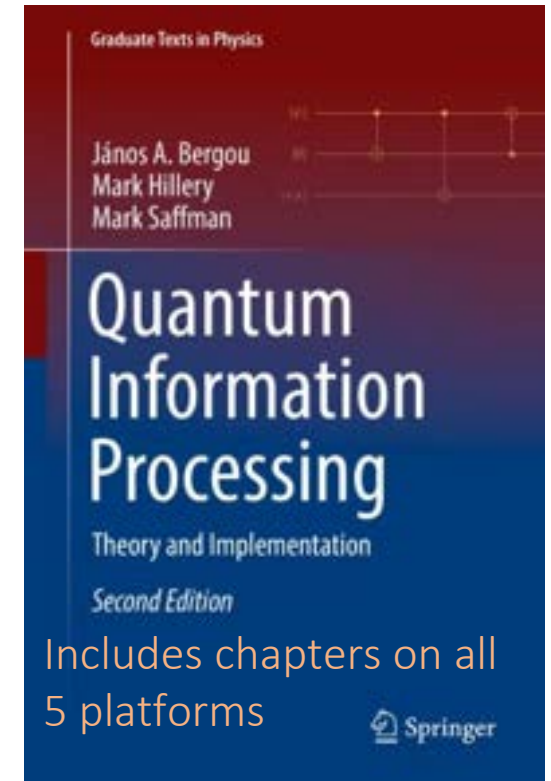


60Q chips

quantum dots



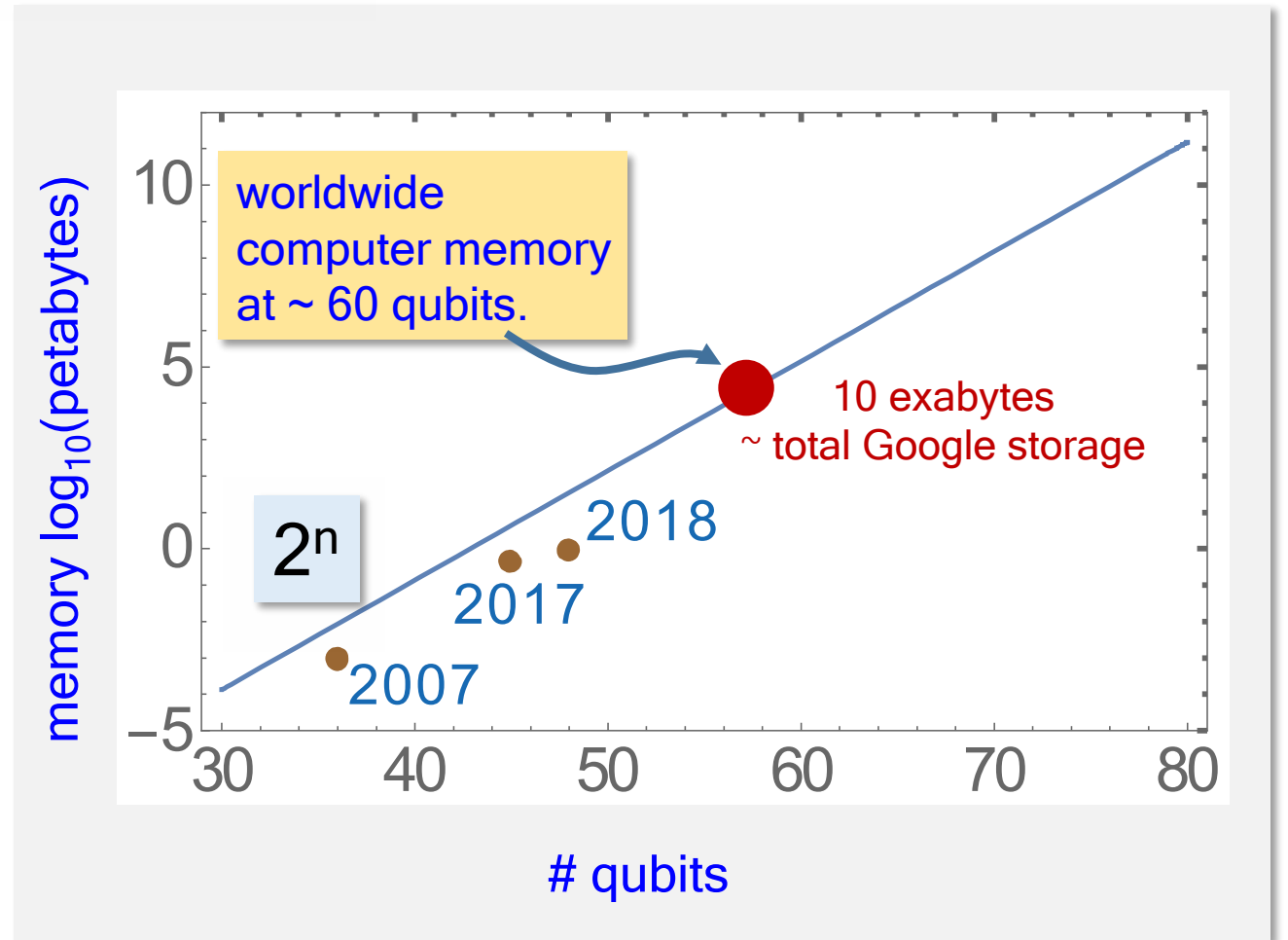
2Q devices



Classical Simulation of Quantum Circuits

Large scale classical simulators are memory or time limited.

Brute force requires exponential memory



2007 Massively parallel quantum computer simulator *Comp. Phys. Commun.* 176, 121 (2007) [1 terabyte](#)

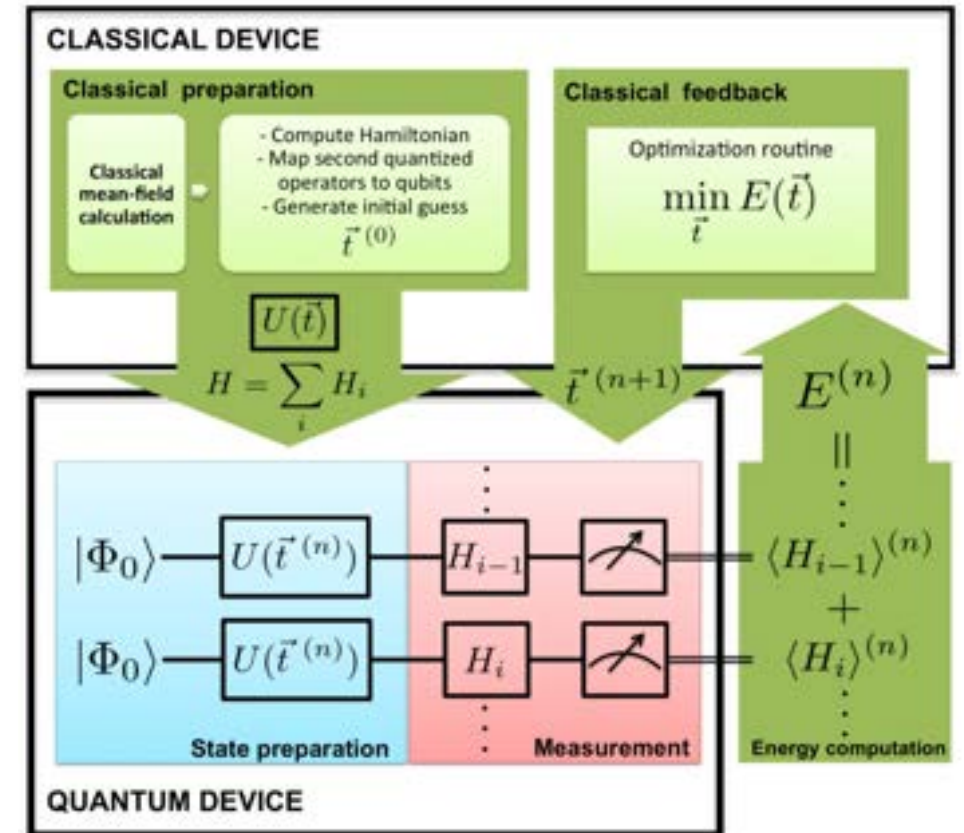
2017 0.5 Petabyte Simulation of a 45-Qubit Quantum Circuit [arXiv: 1704.01127](#) [0.5 petabytes](#)

2018 Massively parallel quantum computer simulator, eleven years later [arXiv: 1805.04708](#) [1.0 petabytes](#)

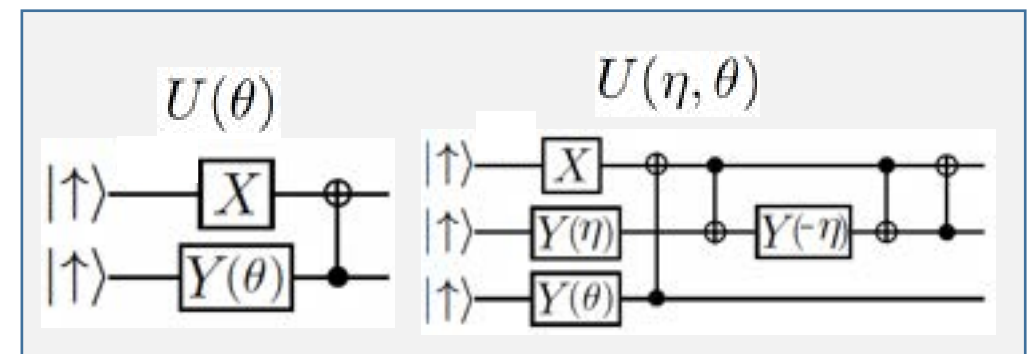
Near term algorithms

- There is still a big gap between the promise of quantum computing and the reality of today's hardware.
- Sometimes referred to as the NISQ era -
Noisy Intermediate Scale Quantum
- A great deal of current effort on hybrid approaches:
classical optimization coupled with a quantum co-processor.
VQE - Variational quantum eigensolver
QAOA - Quantum Approximate Optimization Algorithm
- These approaches can be used for quantum machine learning.

- Quantum hardware for state preparation and measurement of observables.
- Classical processing for analysis of the quantum measurements and optimal choice of the state ansatz to find a variational optimal.



Dumitrescu, et al. Cloud Quantum Computing of an Atomic Nucleus, PRL **120**, 201501 (2018)



J. S. Otterbach, R. Manenti, N. Alidoust, A. Bestwick, M. Block, B. Bloom, S. Caldwell, N. Didier, E. Schuyler Fried, S. Hong, P. Karalekas, C. B. Osborn, A. Papageorge, E. C. Peterson, G. Prawiroatmodjo, N. Rubin, Colm A. Ryan, D. Scarabelli, M. Scheer, E. A. Sete, P. Sivarajah, Robert S. Smith, A. Staley, N. Tezak, W. J. Zeng, A. Hudson, Blake R. Johnson, M. Reagor, M. P. da Silva, and C. Rigetti
Rigetti Computing, Inc., Berkeley, CA
(Dated: December 18, 2017)

Clustering of input data is a well known unsupervised learning task.

This can be mapped onto a combinatorial optimization problem called MaxCut.

Given a graph divide the vertices into two sets such that the number of connections between vertices in different sets is maximized.

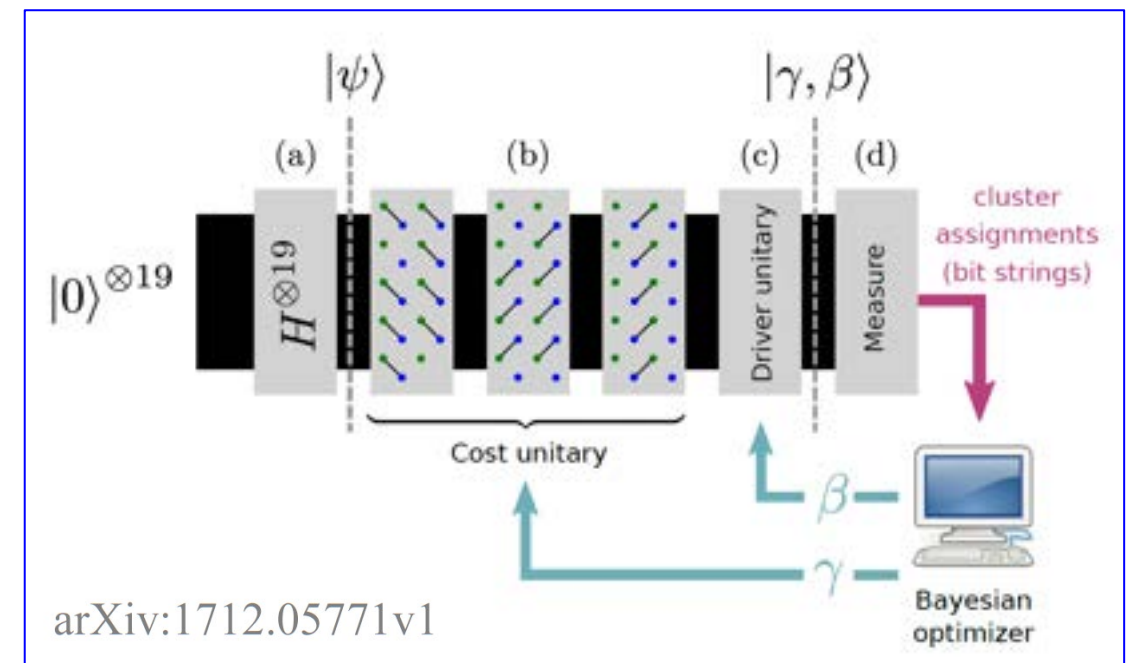
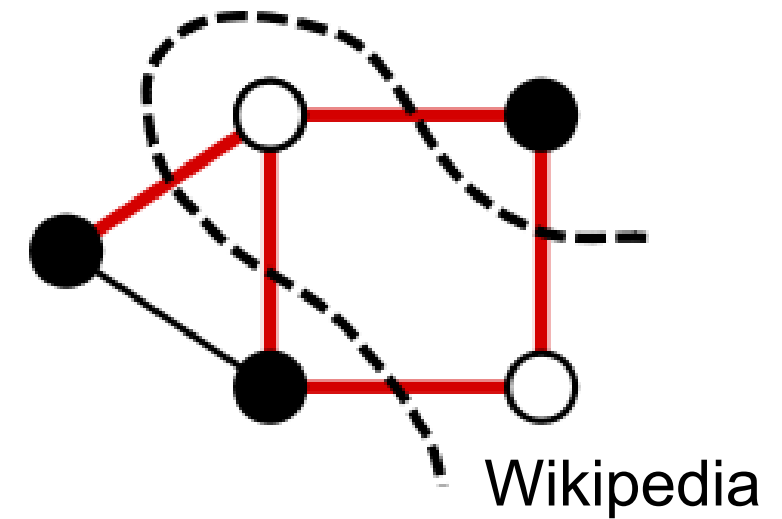
MaxCut

Example of MaxCut for a 5 vertex graph.

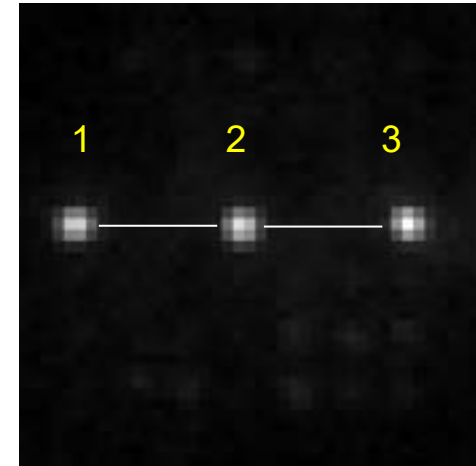
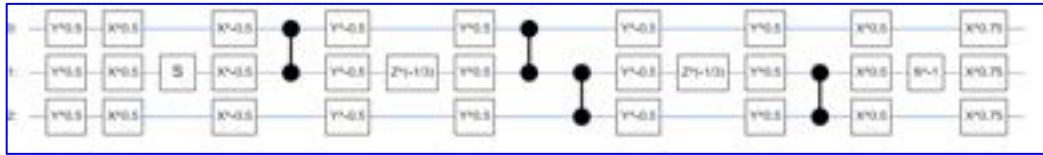
For the clustering application – weighted MaxCut is used where the weight function is a distance metric between objects.

MaxCut is NP hard, but there are efficient classical heuristics.

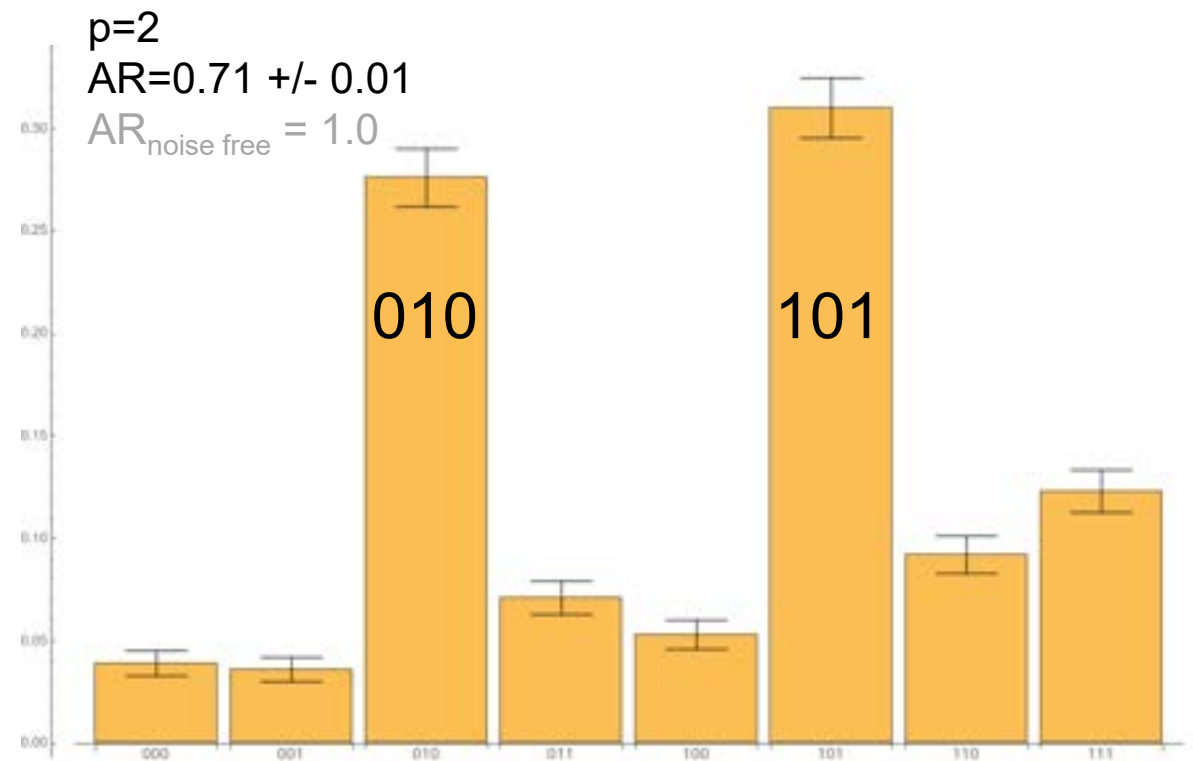
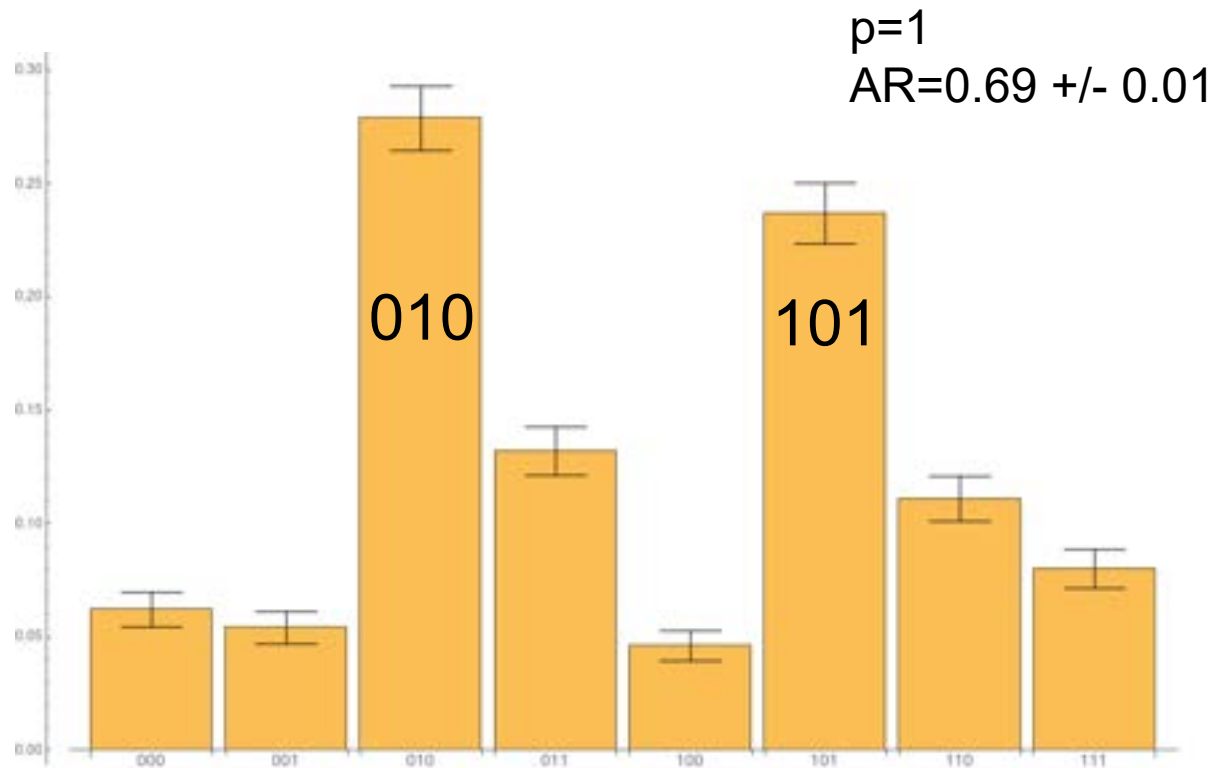
QAOA (generalization of VQE) can be used to directly solve MaxCut on quantum hardware.



- QAOA for 3 node MaxCut



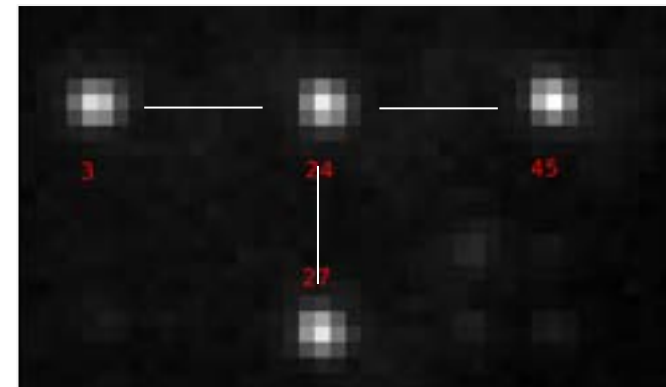
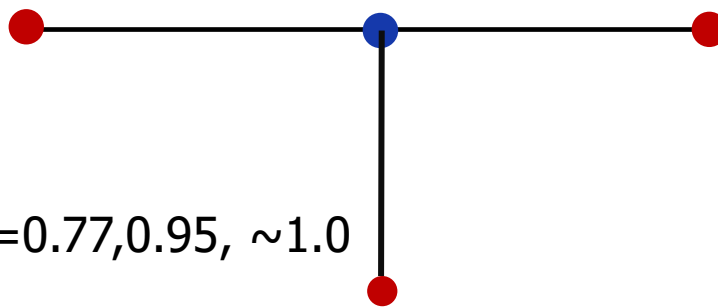
MaxCut solutions are 010 and 101



QAOA MaxCut – 4 qubits

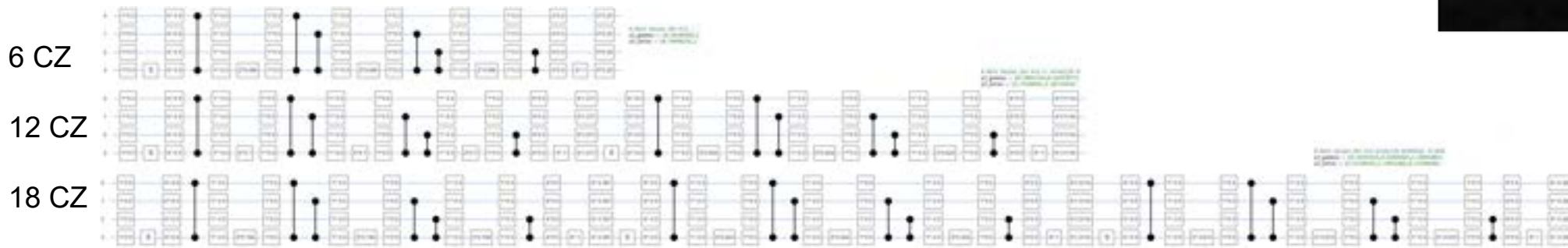
arXiv: 2112.14589

- QAOA for 4 node MaxCut

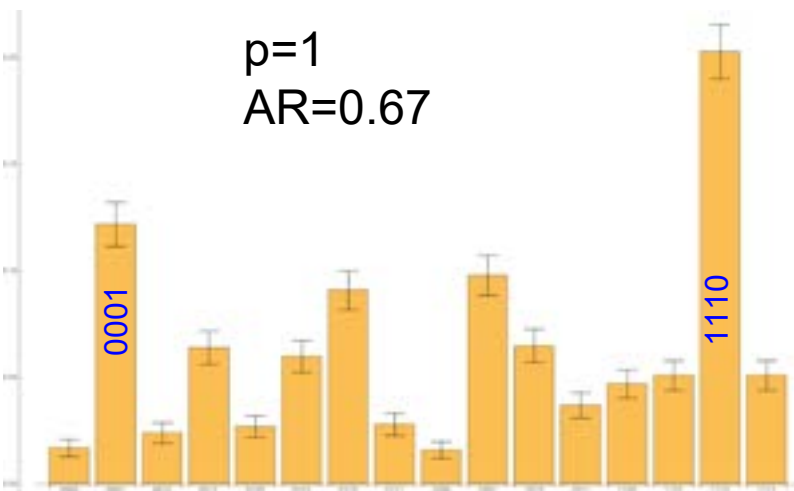


MaxCut solutions are 0001 and 1110

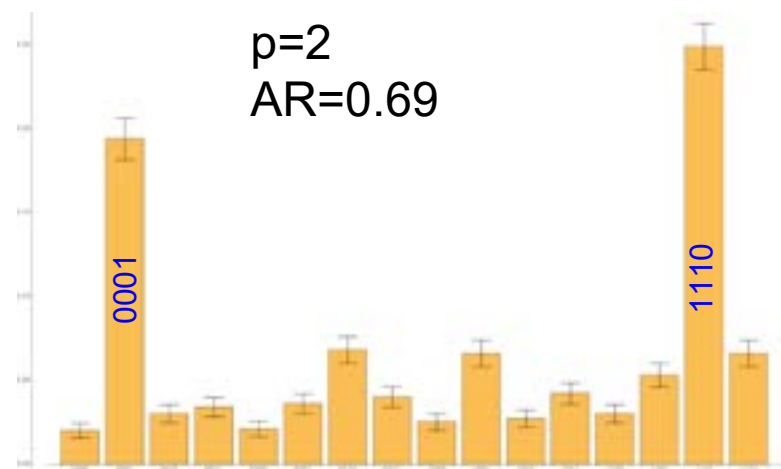
Noise free prediction for $p=1,2,3$ is $AR=0.77, 0.95, \sim 1.0$



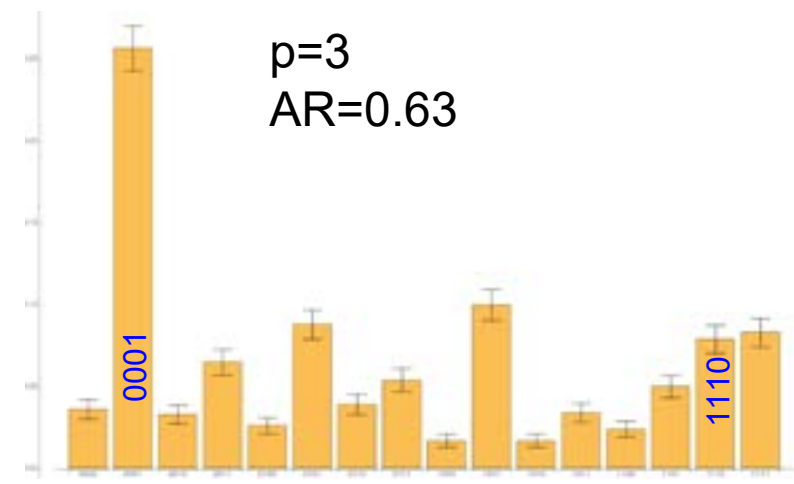
$p=1$
 $AR=0.67$



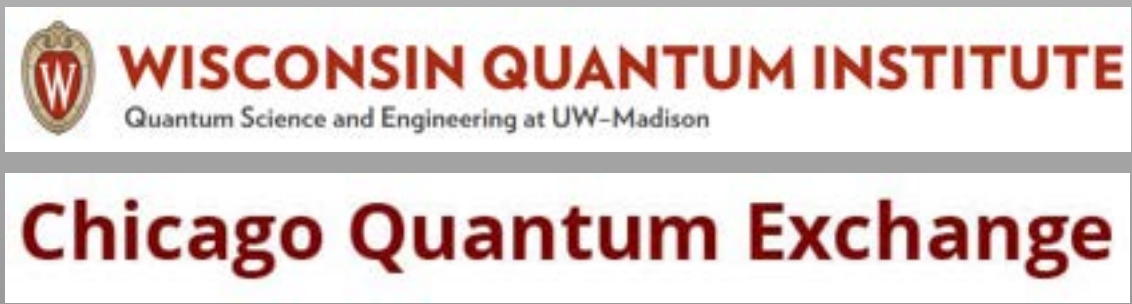
$p=2$
 $AR=0.69$



$p=3$
 $AR=0.63$



Quantum Science and Engineering at UWM



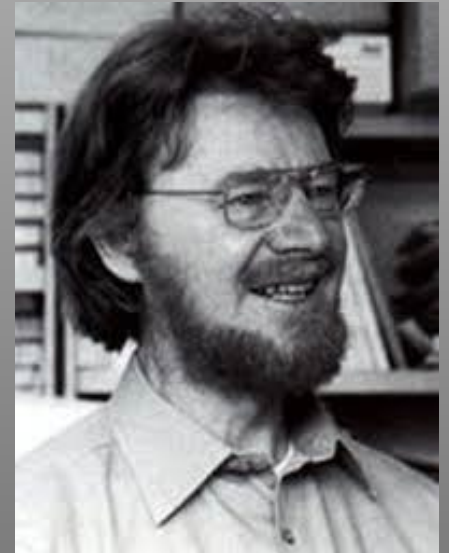
Early days

Physics Vol. 1, No. 3, pp. 195–200, 1964 Physics Publishing Co. Printed in the United States

ON THE EINSTEIN PODOLSKY ROSEN PARADOX*

J. S. BELL[†]

(Received 4 November 1964)



Susan Coppersmith 2001
Quantum dot qubits



Mark Eriksson 1999
Quantum dot qubits



Dieter van Melkebeek 2000
Computational complexity



Mark Saffman 1999
Neutral atom qubits



29
faculty

Physics, Chemistry, Computer Sciences, Electrical & Computer Engineering,
Engineering Physics, Materials Science, Mathematics, Statistics



Research portfolio

Qubits & Quantum computing

Quantum networking

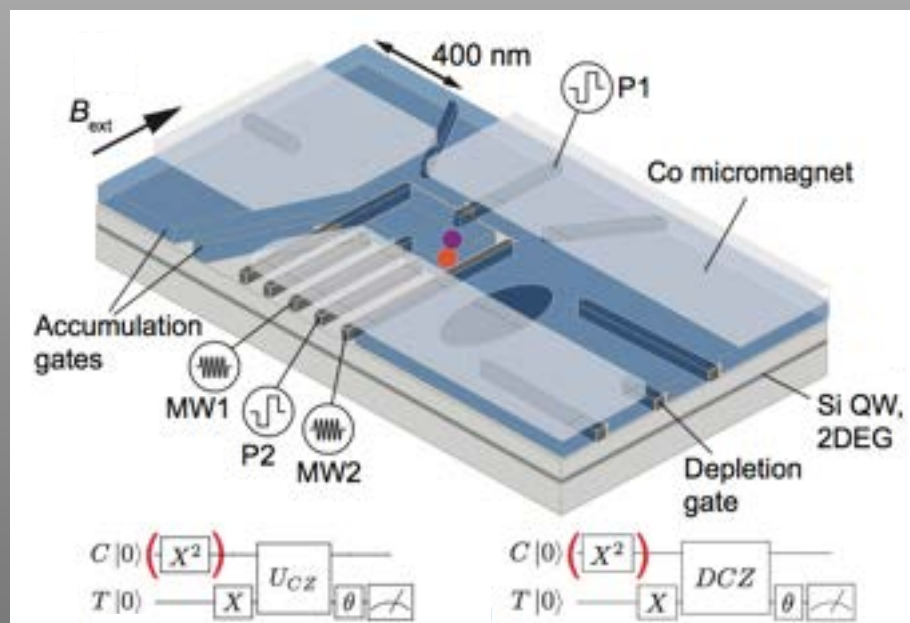
Quantum sensing & metrology

Applications

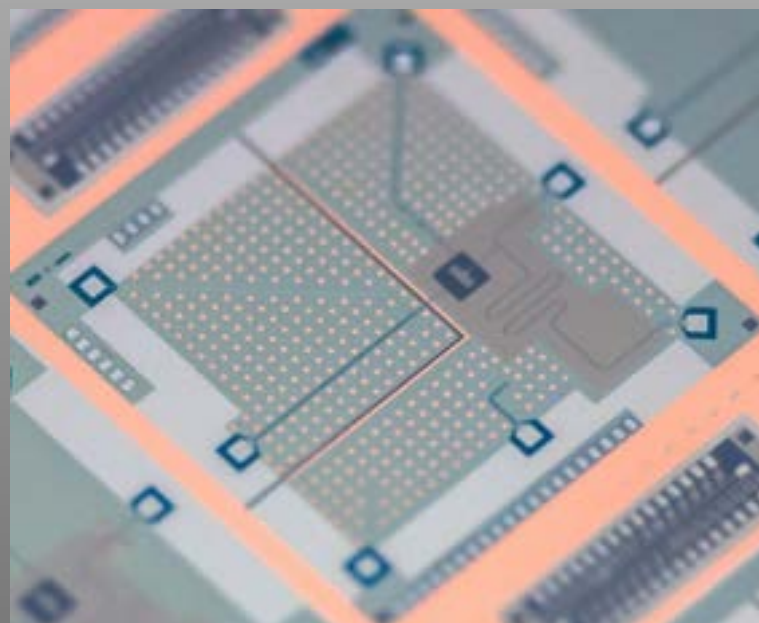
Workforce Development

Qubit platforms

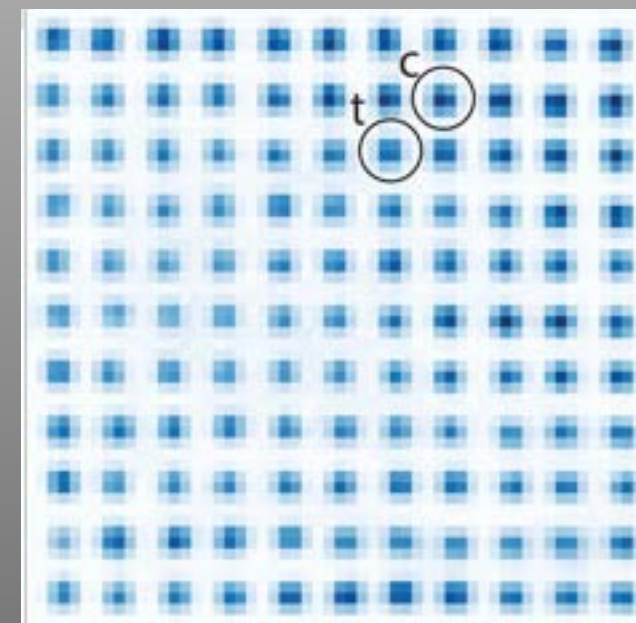
Si quantum dots

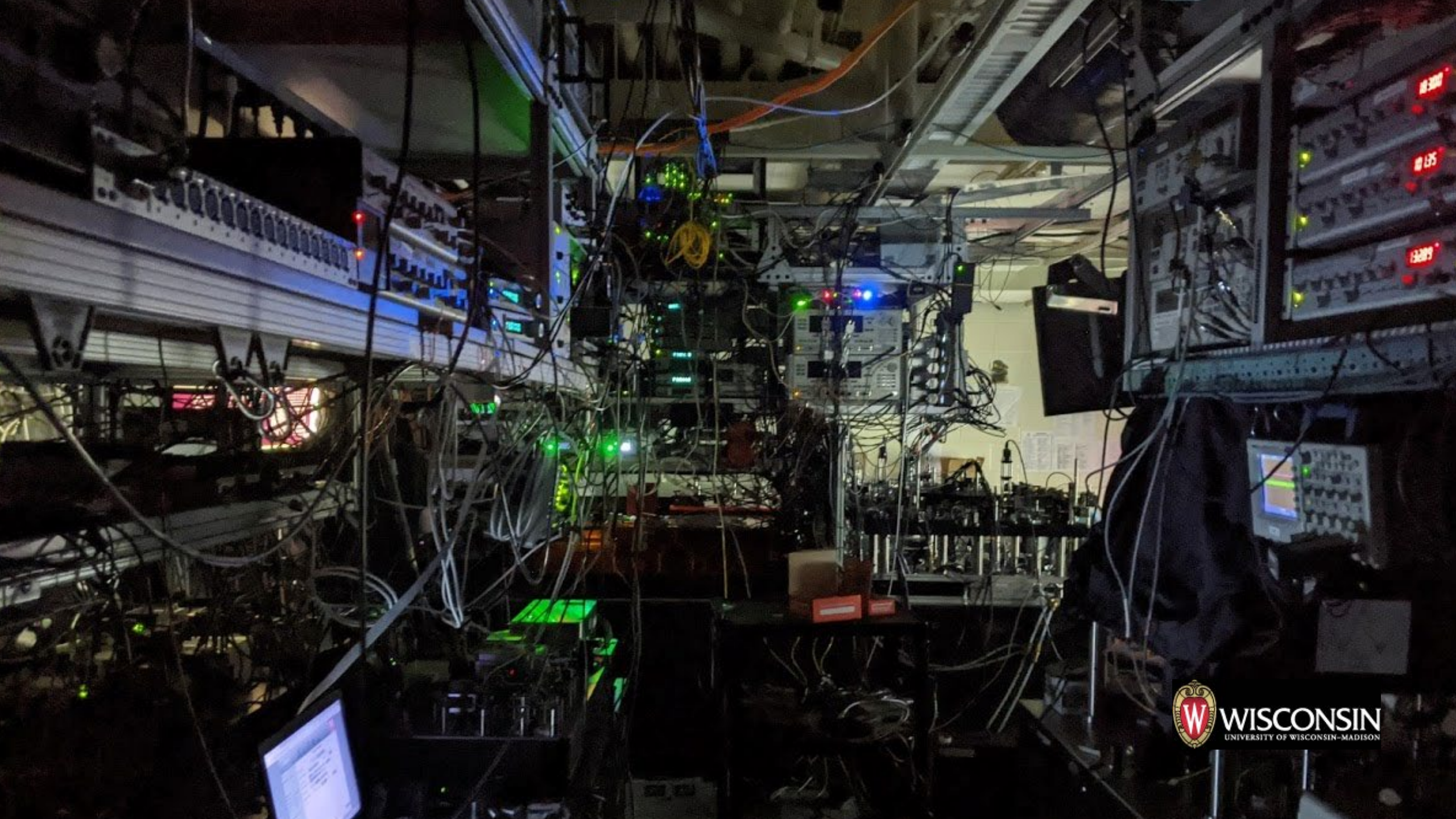


Superconducting circuits



Neutral atom arrays



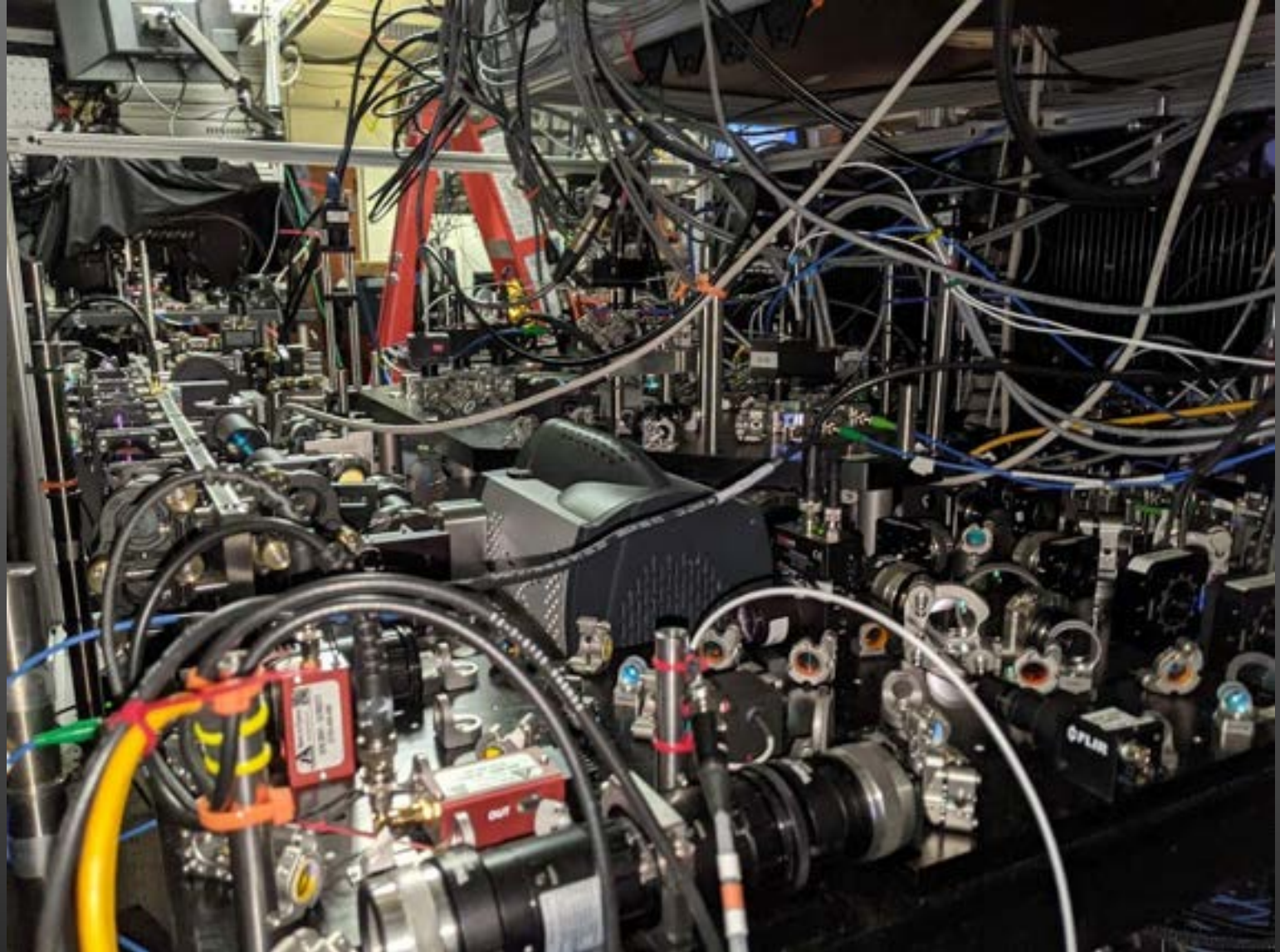


Neutral atom hardware

Inside view of the “QPU” at UWM.

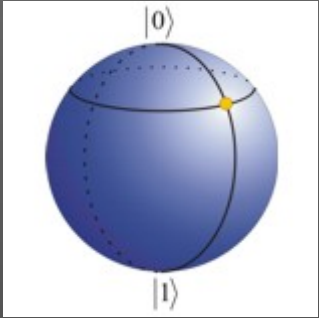
Includes optical components, optomechanics, beam steering, detectors, cameras, all in an enclosure with environmental stabilization.

Not shown are laser, optical, electronic, and computer subsystems that feed into the QPU.



Neutral atom approach

Qubits



- **Initialization** Laser cooling and trapping
- **Coherence** Hyperfine clock states. Coherence > 10s demonstrated
- **Measurements** Light scattering. High fidelity.
- **Universal set of logical gates** Microwaves/laser pulses/Rydberg states
- **Scalability**..... Qubit arrays demonstrated in 1D, 2D and 3D geometries. Several groups have shown arrays with >100 qubits.

DiVincenzo

Fortschr. Phys. (2000)

Qu. Inf. Comp. (2001)

Which atom should we pick ?

Periodic table of laser cooling

1 H																1 H	2 He
3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba	57 La	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra	89 Ac	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt									
		58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu		
		90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr		

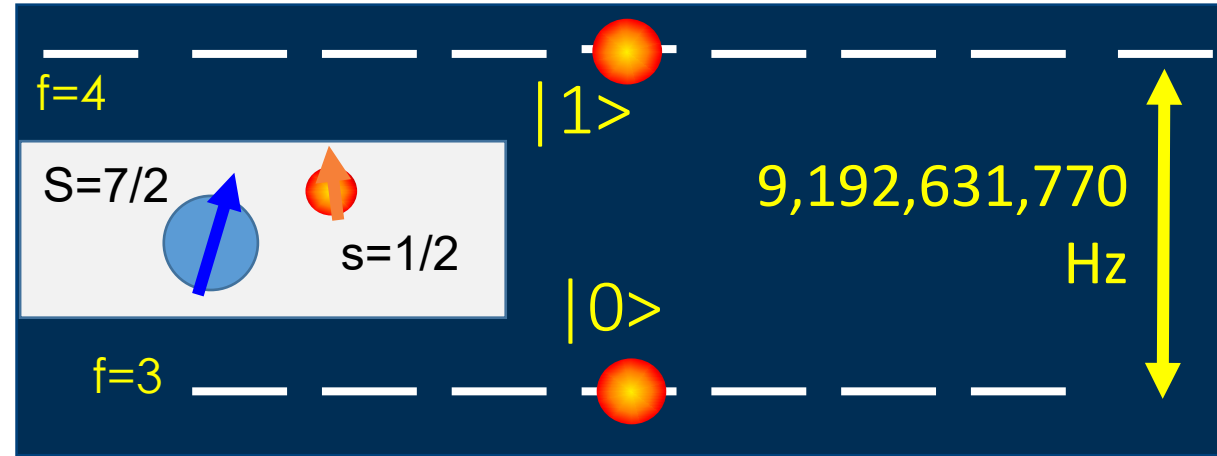
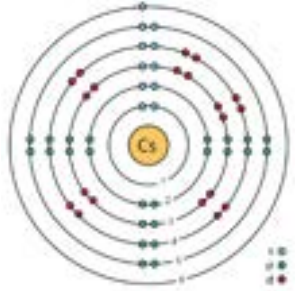
Single atom
arrays:

Rb, Cs,

Sr, Yb

An industry standard qubit

Cesium



- The hyperfine $m=0$ clock states provide the SI definition of the second.
- These states are entangled superpositions of nuclear and electronic spin projections

$$|1\rangle = \uparrow\downarrow + \downarrow\uparrow$$

$$|0\rangle = \uparrow\downarrow - \downarrow\uparrow$$

Excellent coherence properties:

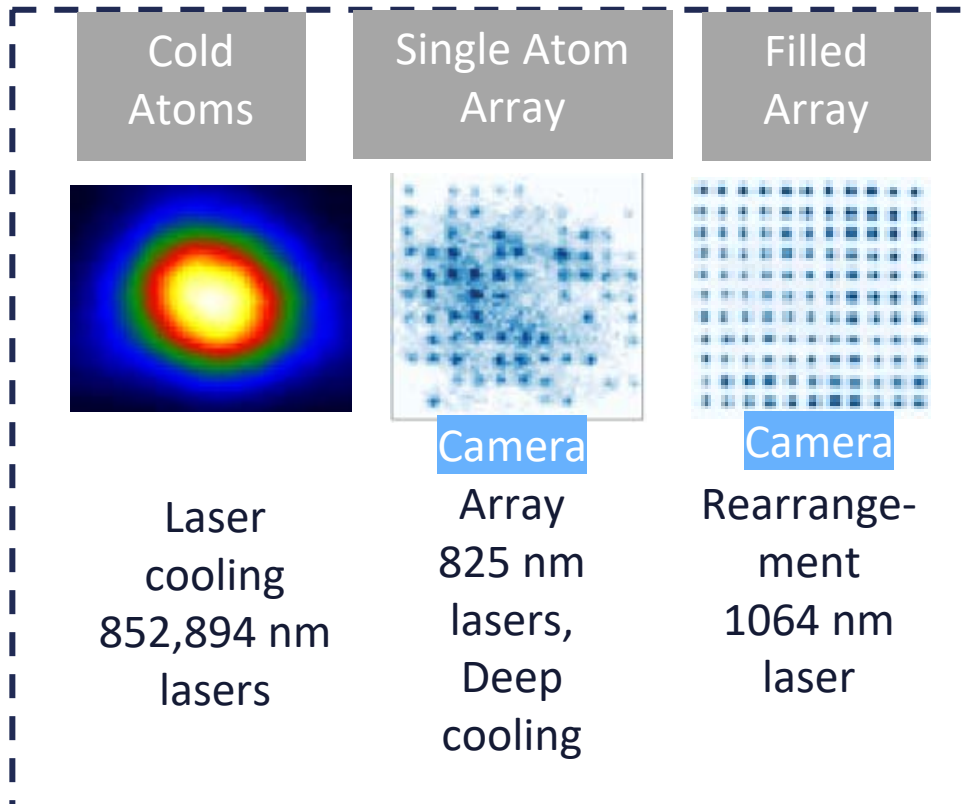
- In free space hyperfine lifetime 34 years
- When optically trapped T1, T2 up to 10s has been demonstrated

Coherence limited by finite atom temperature, trap light optical Stark shifts, magnetic fields.

Minute scale coherence appears possible.

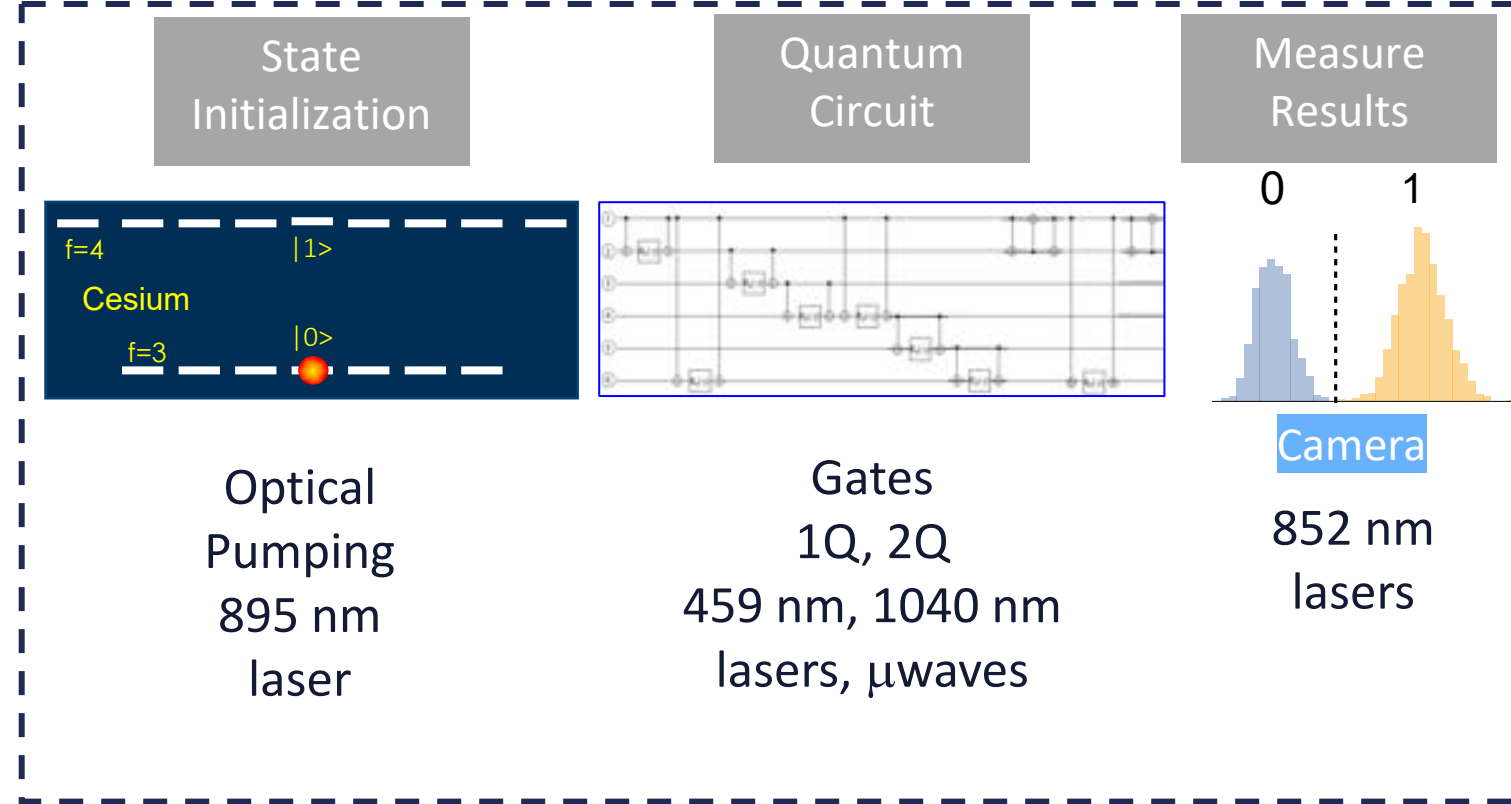
Operational Sequence

Qubit Register Preparation



Controlling the Mechanics

Calculation Cycle

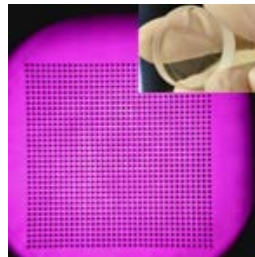


Controlling the Quantum

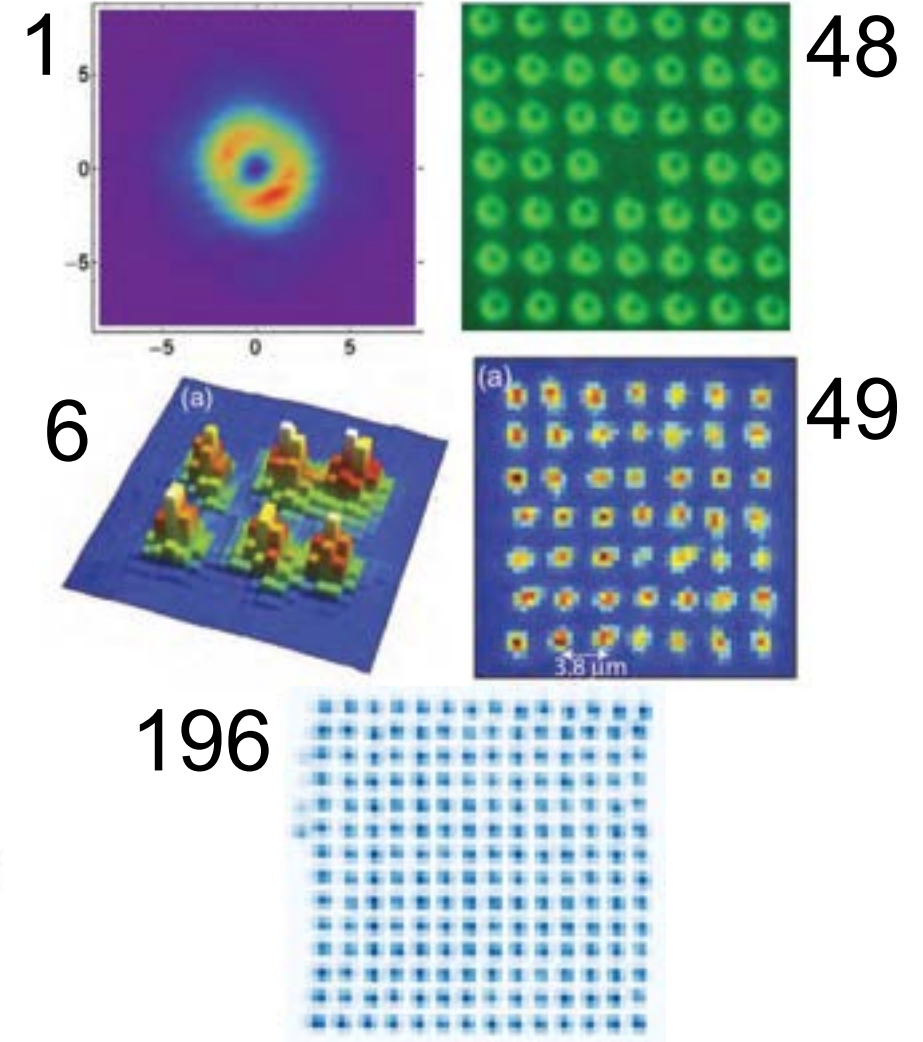
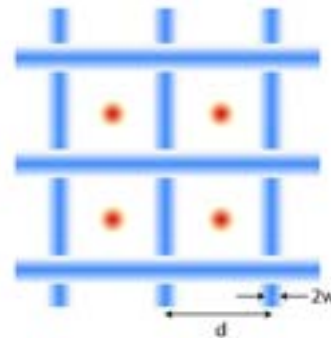
Blue Array Technology

- a single bottle beam Opt. Lett. **34**, 1159 (2009)
- bottle beam array SPIE **8249** (2012)
- Gaussian beam array PRA **88**, 013420 (2013)
- line array PRL **123**, 230501 (2019)
- dynamic line array
- Hole array

>1000 sites



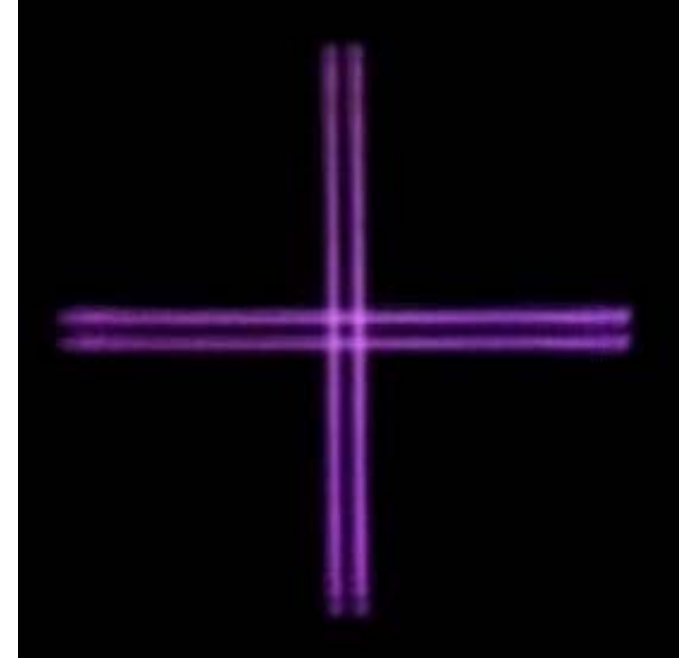
atoms trapped in cages of light



Scalable qubit registers

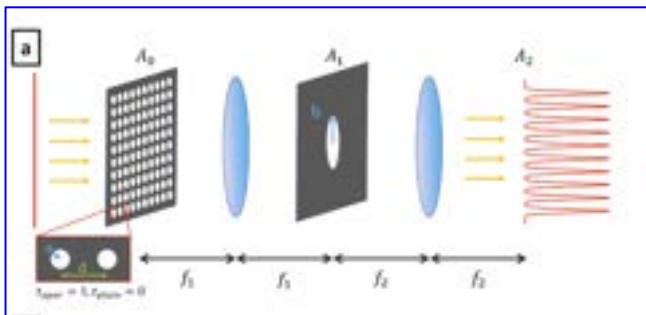
Dynamic line array

Up to 500 sites, currently in use.

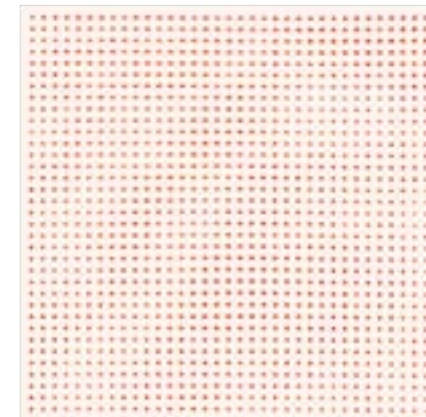
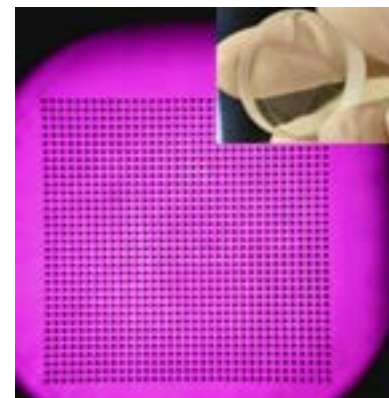


Hole array

Scalable to $>10^4$ sites



Component
1225 sites



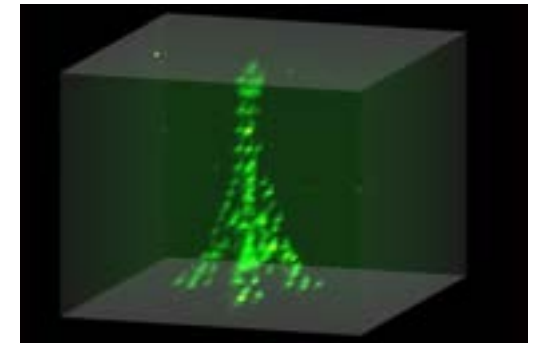
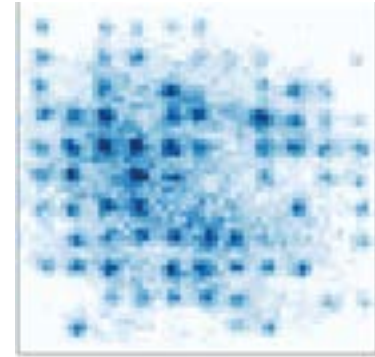
1225
Cs atoms

Atom Rearrangement

- Loading single atoms into a trap array is a stochastic process.
- The array is deterministically filled using “atom rearrangement”.

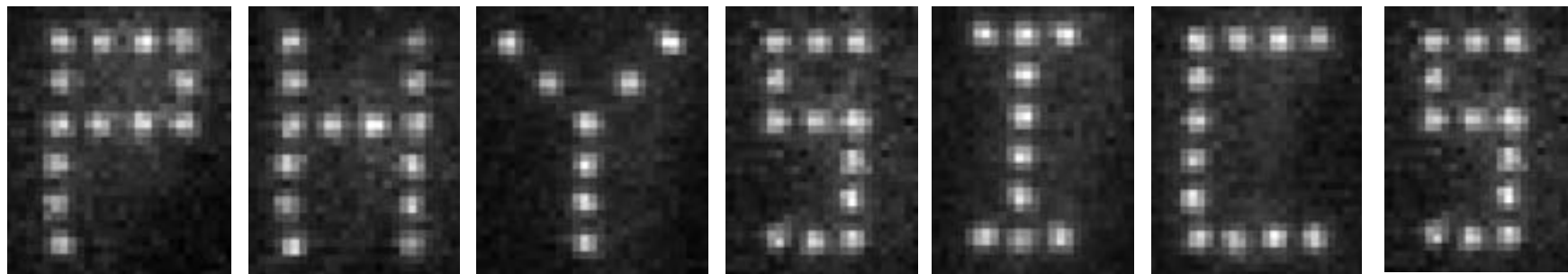
Works in 1D, 2D, 3D

KAIST, Paris, Harvard, Darmstadt, Wuhan, Moscow,



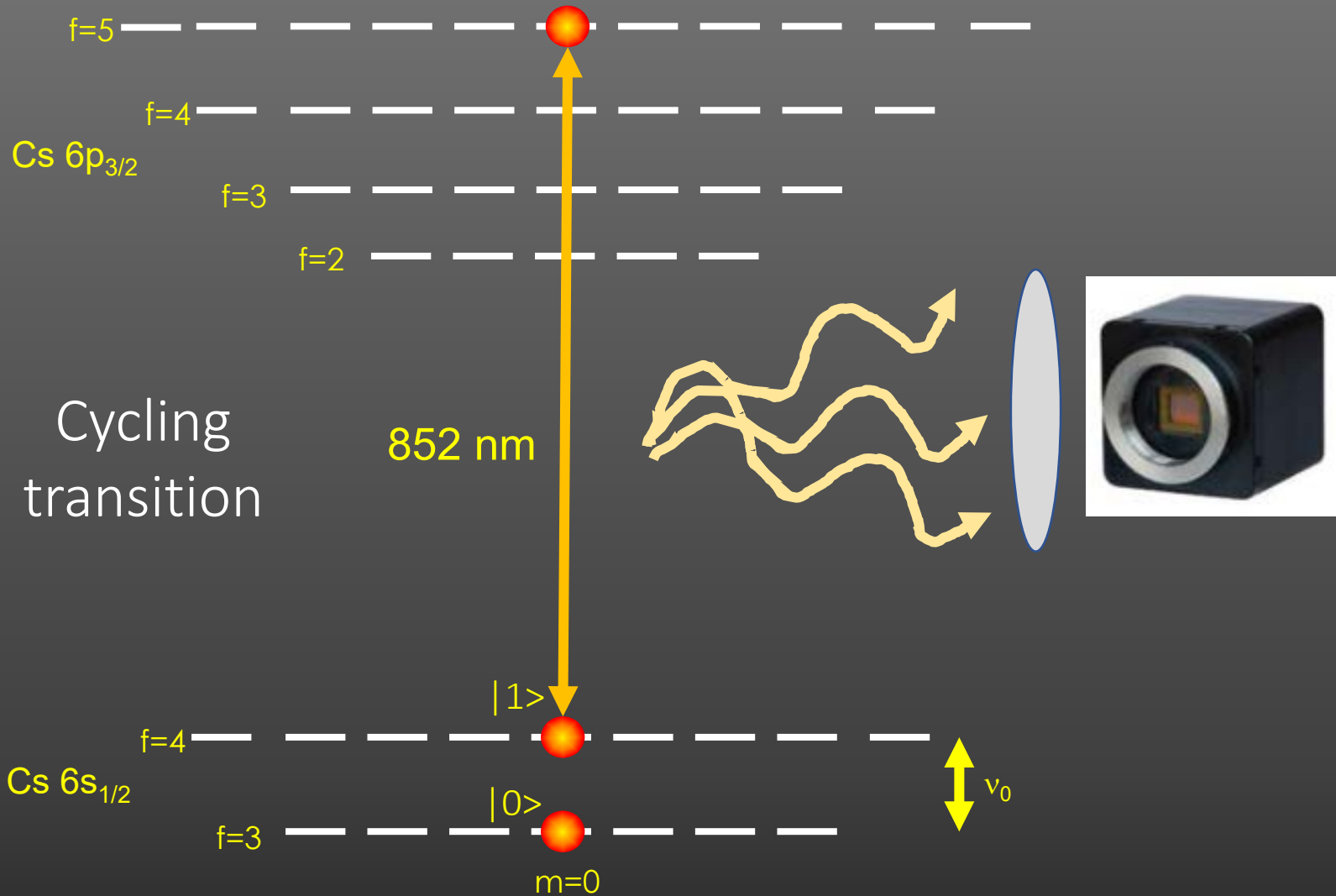
Browaeys group (2019)

2D acousto-optic scanner

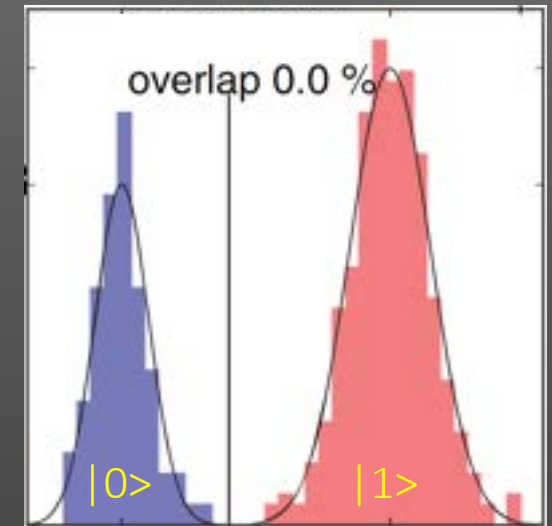


3 μm

Qubit measurement

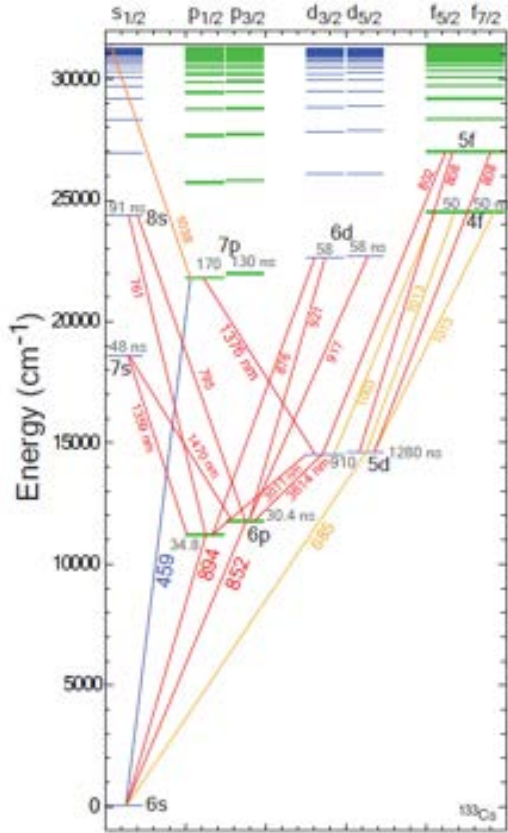


histogram



Photoelectron counts

Qubit control



- 6 different colors
- 13 lasers

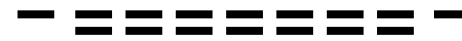
2Q gates

$ns_{1/2}$

$m = -1/2 \quad +1/2$

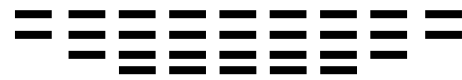
1Q gates

$7p_{1/2}$



cooling, readout

$6p_{3/2}$



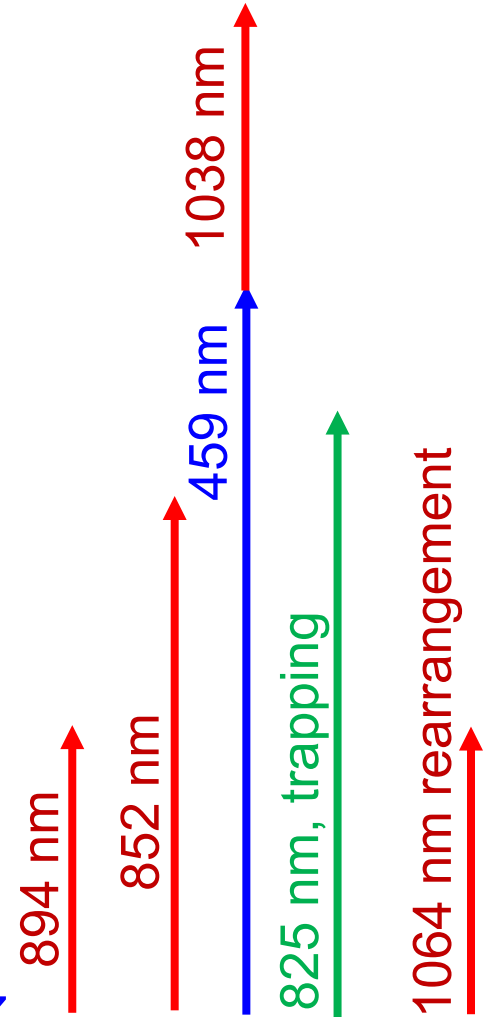
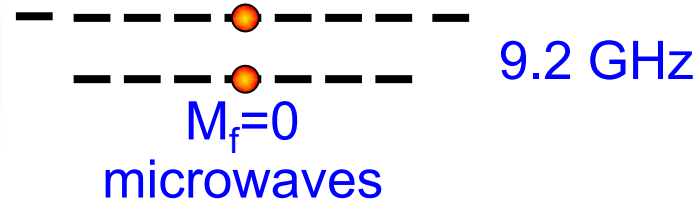
cooling, optical pumping

$6p_{1/2}$



Cs qubit

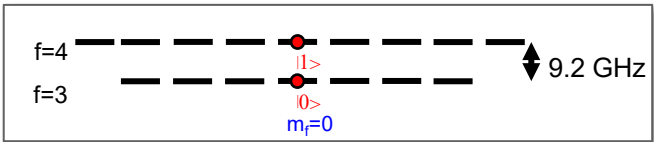
$6s_{1/2}$



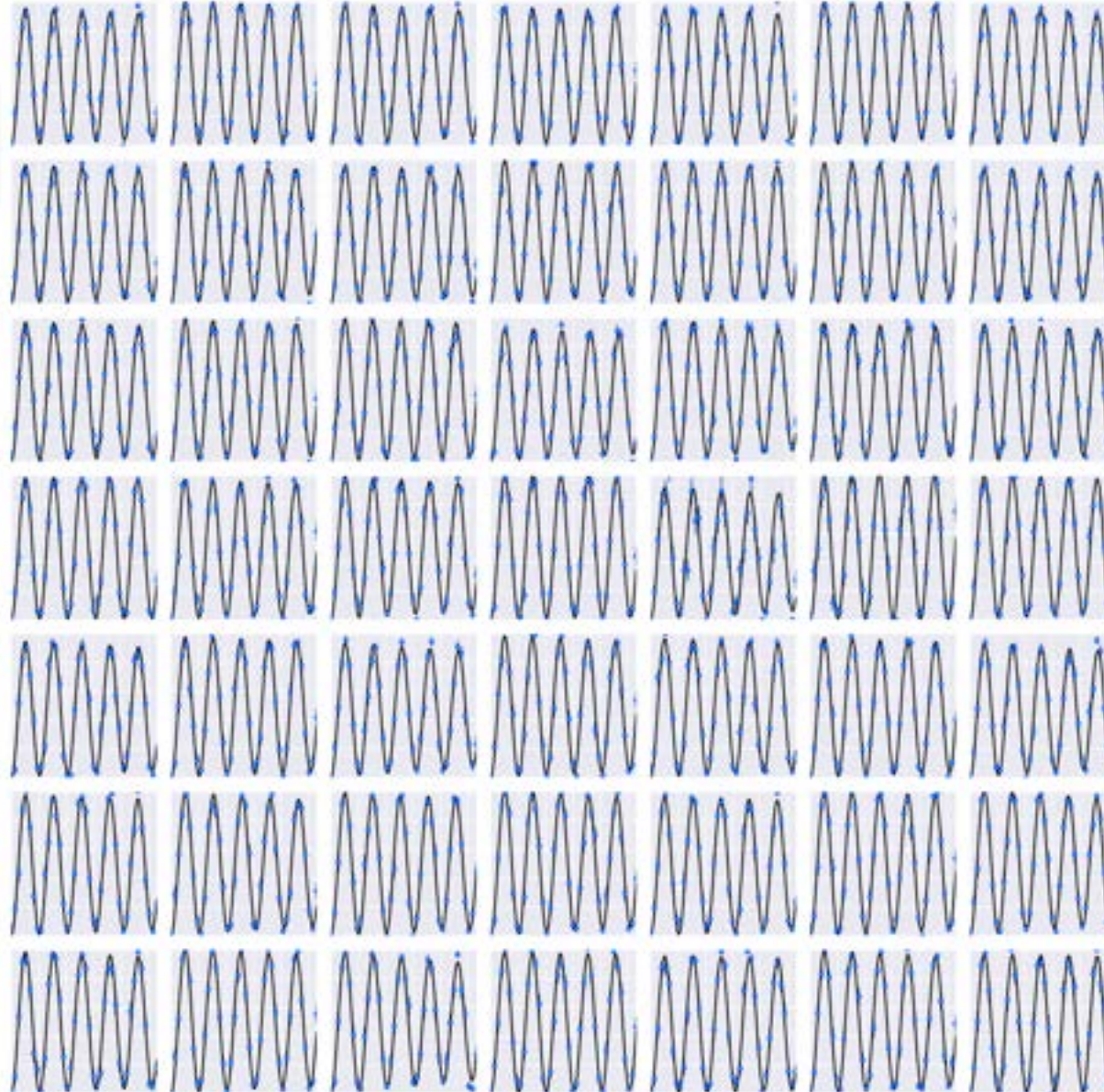
Single qubit gates - global

PRL 114, 100503 (2015)

Cs clock state qubits



Bias field of 1.5 G



Microwaves 10
kHz Rabi
frequency

$\langle F^2 \rangle_{47 \text{ sites}}$	0.9983 ± 0.0014
F^2_{\min}	0.9939 ± 0.0007
F^2_{\max}	0.9999 ± 0.0003



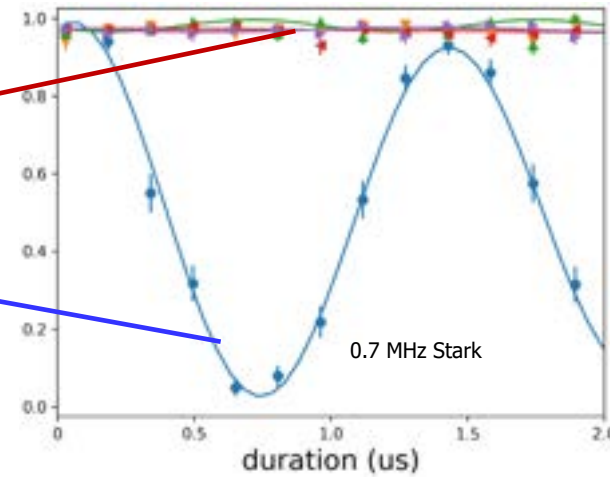
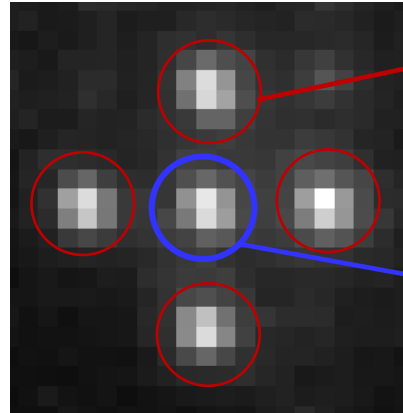
Microwaves 76 kHz
Rabi frequency

Single site control

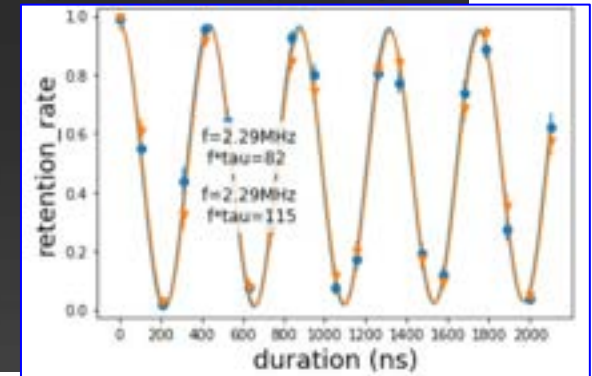
μwave 459 nm μwave
x-talk check: $R_x(\pi/2)$ $R_z(\theta)$ $R_x(-\pi/2)$

Site spacing 3 μm

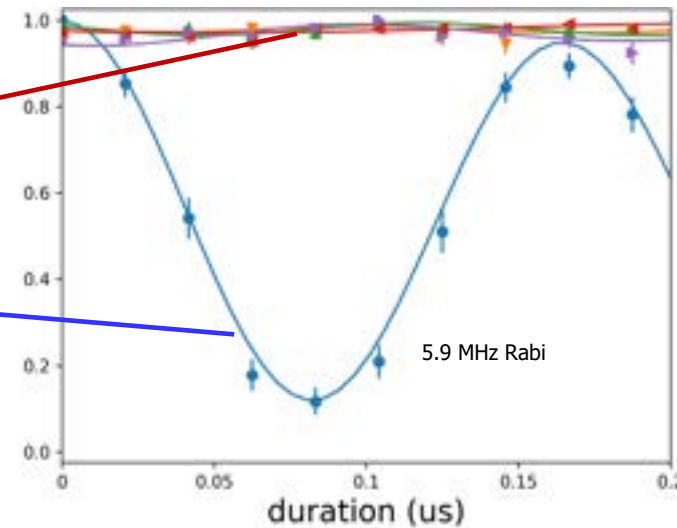
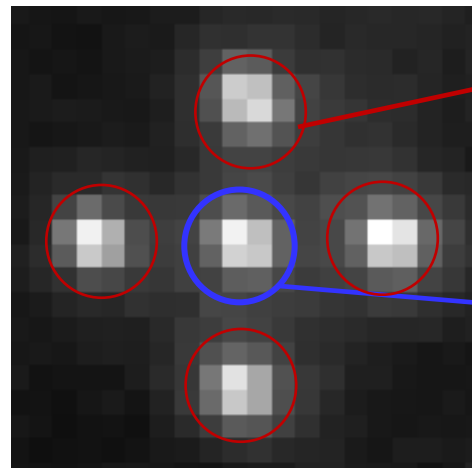
$R_x(\theta)$ rotation on single site



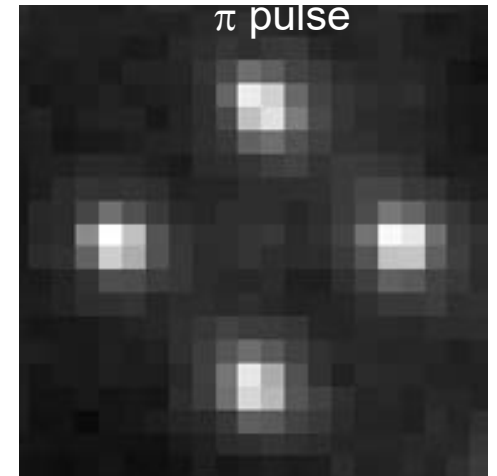
16 site addressing



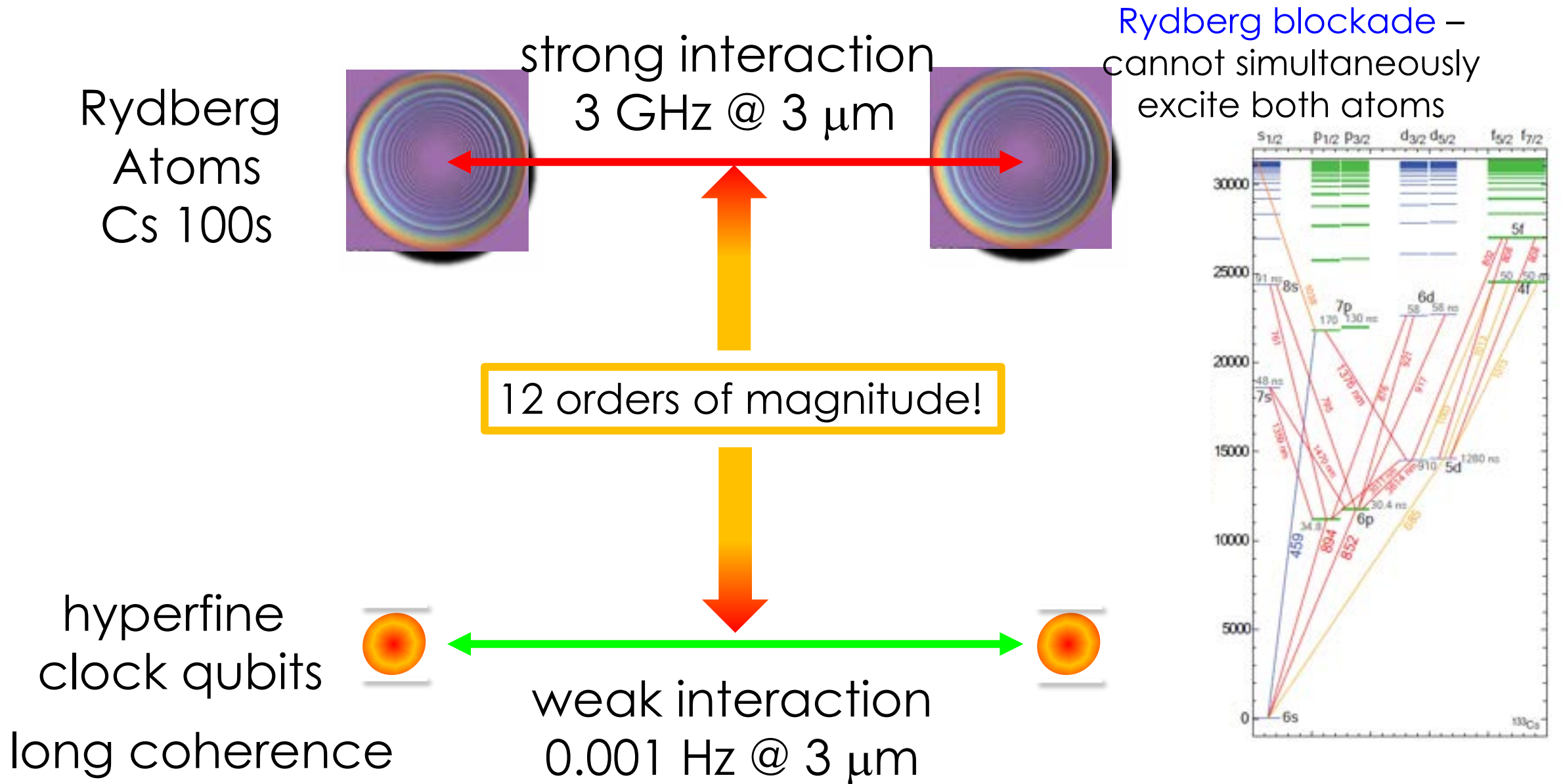
Ground-Rydberg Rabi on central site: 459+1040 nm



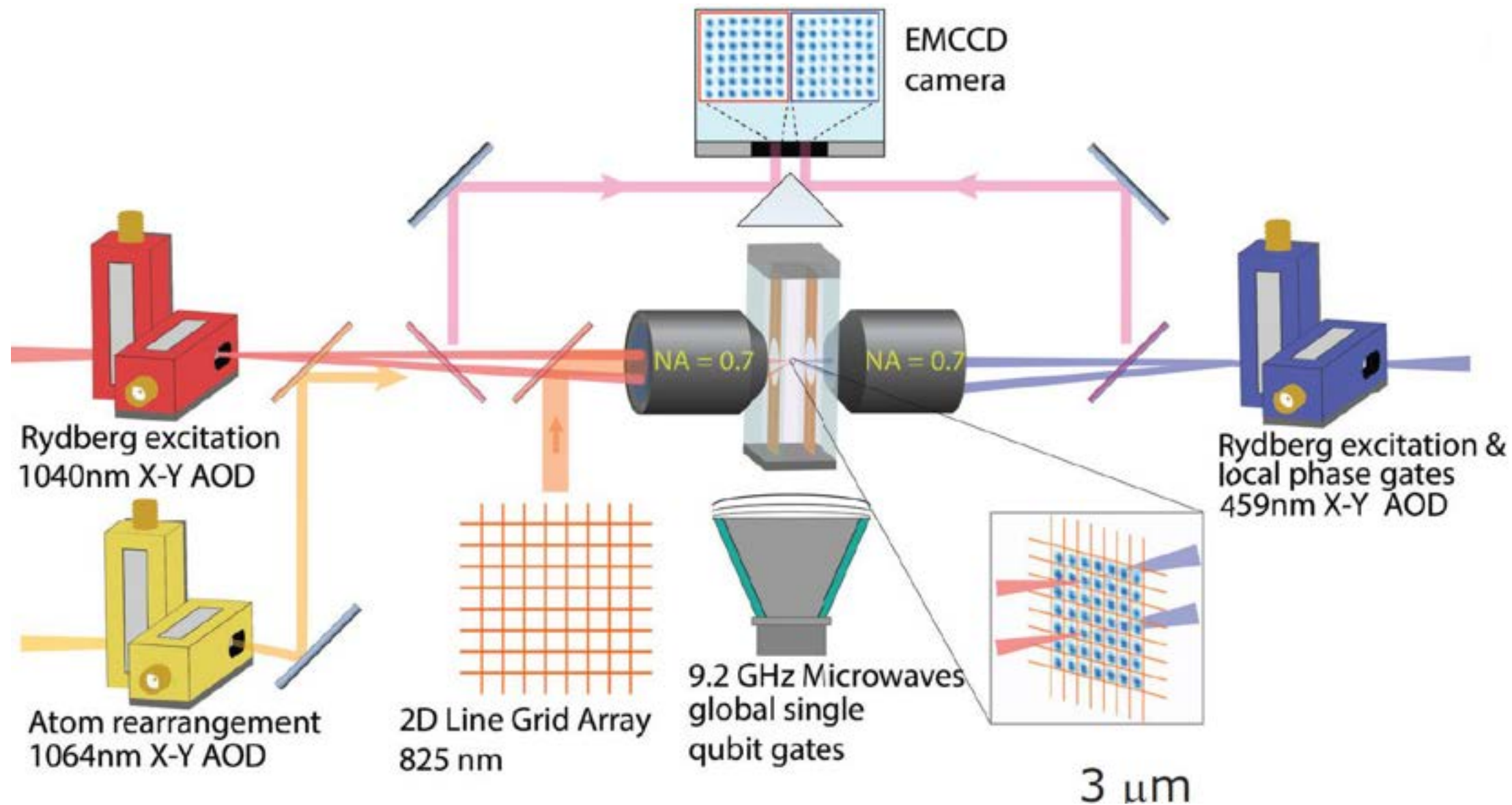
π pulse



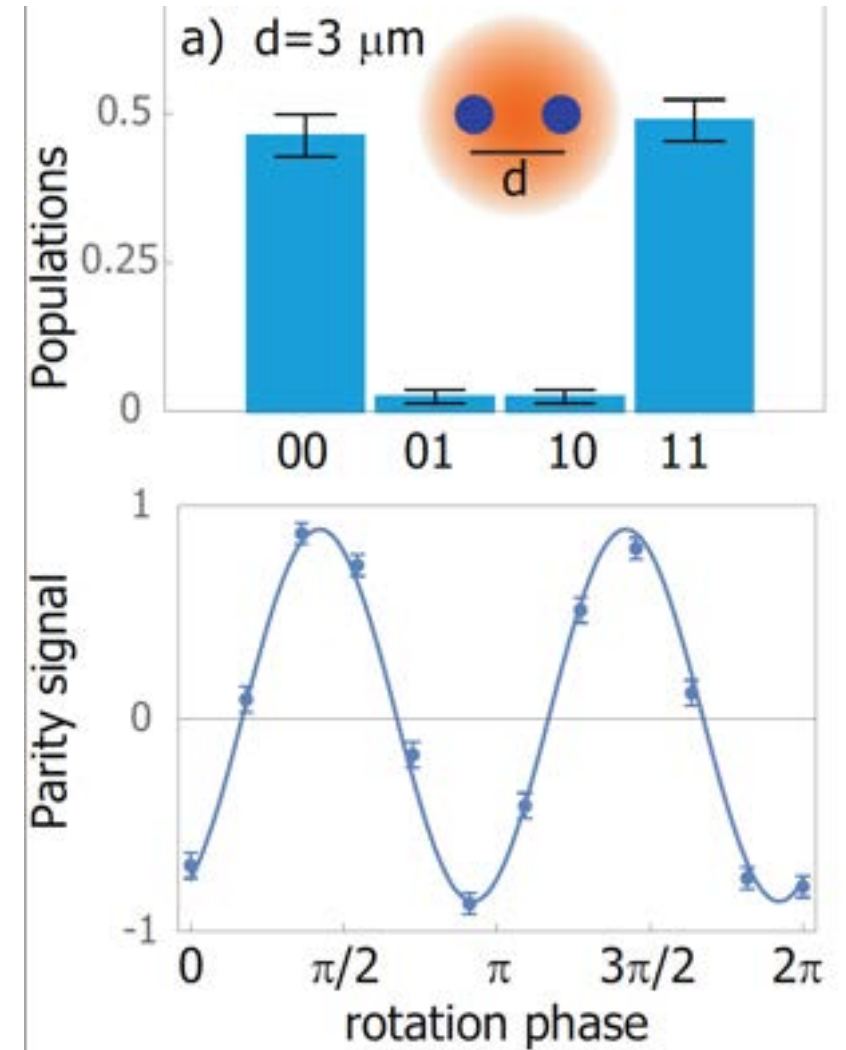
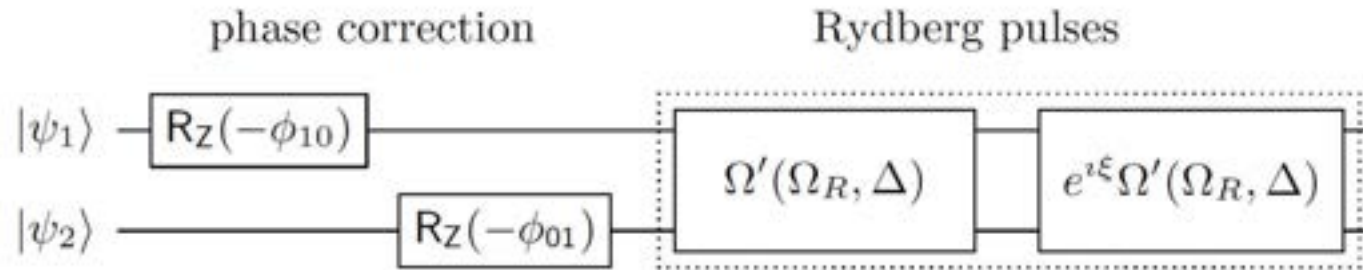
Atomic interactions and Rydberg atoms

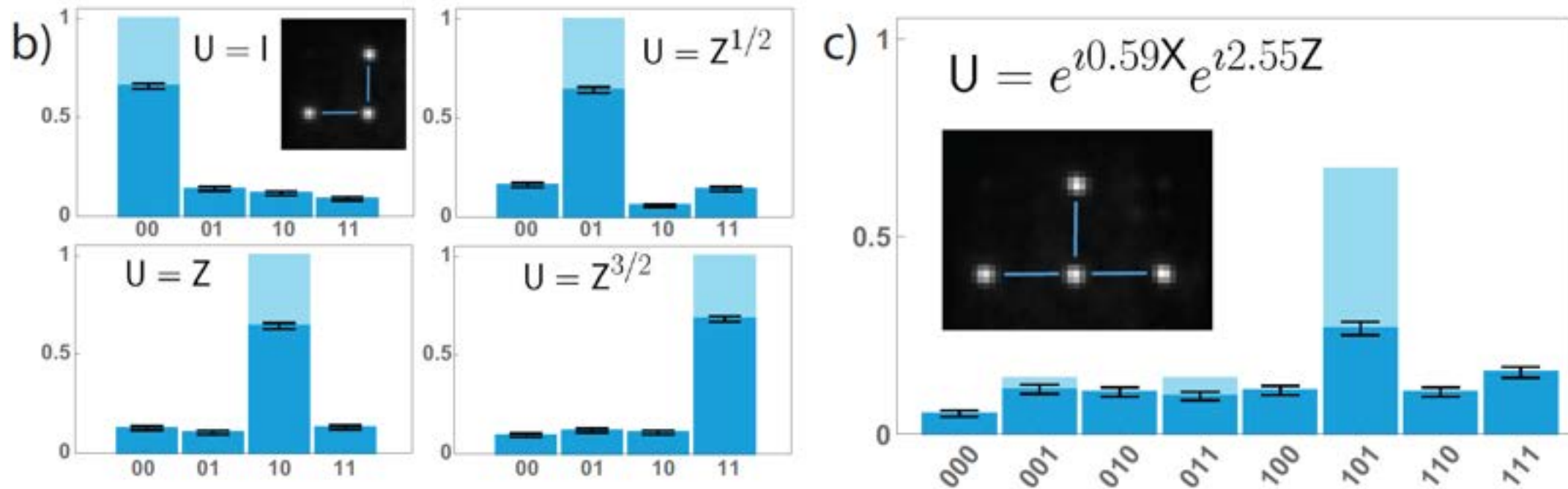
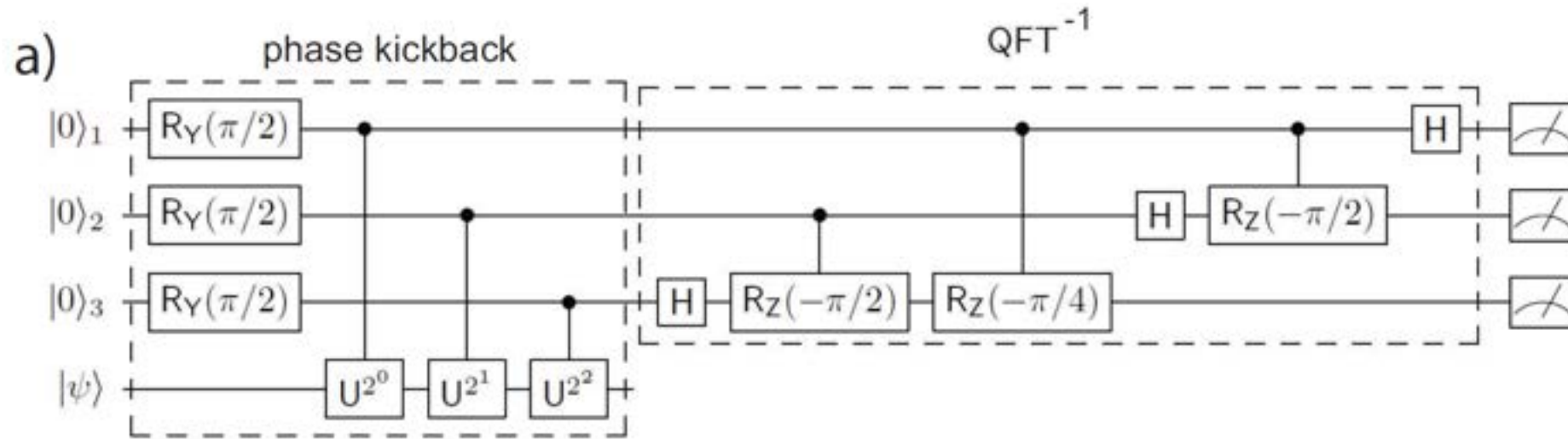


Experimental geometry



Fidelity $F=0.955$





Summary

Quantum computing is a revolutionary approach to information processing.

There is great potential for solving hitherto intractable problems.

Quantum hardware is primitive, but under rapid development.

Hybrid approaches – classical optimizers with quantum co-processors are a near term opportunity.



Wisconsin Alumni Research Foundation